# Finding Aggregate Nearest Neighbor Efficiently without Indexing 

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#### Abstract

Aggregate Nearest Neighbor Queries are much more complex than Nearest Neighbor queries, and pruning strategies are always utilized in ANN queries. Most of the pruning methods are based on the data index mechanisms, such as R-tree. But for the wellknown curse of dimensionality, ANN search could be meaningless in high dimensional spaces. In this paper, we propose two nonindex pruning strategies in ANN queries on metric space. Our methods utilize the r-NN query and projecting law, analyze the distributing of query points, find out the search region in data space, and get the result efficiently.


## Categories and Subject Descriptors

H. 2 [Database Management]; H3.3 [Information Storage and

Retrieval]: Information Search and Retrieval
General Terms: Algorithms, Experimentation

## Keywords

Spatial database, Aggregate Nearest Neighbor, Search Region

## 1. INTRODUCTION-MOTIVATION

Given the static source dataset $\mathrm{P}=\left\{\mathrm{p}_{1}, \mathrm{p}_{2}, \ldots \mathrm{p}_{\mathrm{N}}\right\}$ and the query points set $\mathrm{Q}=\left\{\mathrm{q}_{1}, \mathrm{q}_{2}, \mathrm{q}_{3} \ldots \ldots, \mathrm{q}_{\mathrm{n}}\right\}$, an ANN query retrieves the point in P which minimizes an aggregate distance function with respect to all the points in query set Q . The aggregate distance between a data point and query points set Q can be expressed by $\operatorname{adist}(\mathrm{p}, \mathrm{Q})=\mathrm{f}\left(\left|\mathrm{pq}_{1}\right|,\left|\mathrm{pq}_{2}\right|, \ldots,\left|\mathrm{pq}_{\mathrm{n}}\right|\right)$, where $\left|\mathrm{pq}_{\mathrm{i}}\right|$ is the Euclidean distance between point $p$ and $q_{i}$. Different function $f$ gives ANN query different meaning. ANN query has received considerable attention the last few years and it has become more and more important in spatial database [1,2,3]. In order to compute as few

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distances as possible, pruning strategies are always used to optimize the query processing in ANN queries, for which many efficient indexing structures have been proposed such as R-tree. But for the well-known curse of dimensionality, the traditional indexing methods are reasonably well solved just for low dimensional applications. Many studies have shown that traditional indexing methods fail in high dimensional space. Thus NN search and ANN search would be meaningless in high dimensional spaces.

In this paper, we propose two non-indexing pruning strategies for ANN query processing which we call them vp-ANN algorithm and projection-based algorithm. We assume that all query points can fit in main memory and only consider the sum function. For the following discussion, we consider 2-Dimendional point datasets. But the proposed techniques are applicable to higher dimension

## 2. PRUNING WITHOUT INDEX

As for the sum function in ANN query, $\operatorname{adist}(\mathrm{p}, \mathrm{Q})=\operatorname{sum}\left(\left|\mathrm{pq}_{1}\right|\right.$, $\left.\left|\mathrm{pq}_{2}\right|, \ldots,\left|\mathrm{pq}_{\mathrm{n}}\right|\right)$, the best ANN point should make the value of distance of $\left|\mathrm{pq}_{\mathrm{j}}\right|_{\mathrm{j}=1 . . \mathrm{n}}$ be as small as possible. It is clearly that the best ANN result would be lie in the region in which the query points distribute concentrically. If the data points in dataset $P$ distribute uniformly in data space. We can say that the result of ANN query (we call it the best ANN point) should be inside the region which the $\operatorname{MBR}$ (Minimum Bounding Rectangle) of the query points set $Q$ covers in data space. In our methods, pruning means we find a search region in data space and get the best ANN point in this region, instead of searching in full data space. Not using the indexing mechanisms, our pruning methods analyze the distributing of query points by different ways, and mark out the search region. The most important technique of our methods is how to find the search region which is equal to or covers the MBR of query points set.

### 2.1 Vp-ANN Algorithm

The ideal best ANN point p would be the point which lets every $\left|p q_{j}\right|_{j=1 . . n}$ be minimal in $\left\{\left|p_{i} q_{j}\right|_{i=1 . . n}\right\}$. This is to say this point would be the Nearest Neighbor of every query point $q_{j}(j=1 . . n)$ synchronously. For the data points of P distribute uniformly and there must be many points in P , we can say this ideal best ANN
point p would not exist indeed. But enlightened by this, we know the best ANN point p would be as near as possible to each query point in Q . Given a point vp and radius r , we describe the r neighbor region of vp by $C(v p, r)=\{p|p \in P,|p v p|<=r\}$. It can be concluded that for every point $q_{i}$ the best ANN point should be in its r-neighbor region. On that we give out Lemmal.

Lemma1. Let $R_{i}=C\left(q_{i}, r_{i}\right)$ be the $r_{i}$-neighbour region of $q_{i}$, and $R=\cup_{i=1 . . n} R_{i}$ be the union area of $R_{i}$. If each $r_{i}$ we choose can guarantee that the intersection of $\cap_{i=1 . . n} R_{i}$ is not empty, the best ANN point must be in $R$.

The R in Lemma1 is the search region of our vp-ANN algorithm. Now the most important thing for us is to consider each $r_{i}$ carefully. For simplifying the process, we choose a point vp in dataset $P$, and select the Euclidean distance between vp and $q_{i}$ to be $r_{i}$. The focus converts to how to select the pivot vp. We know the aggregate centroid of $Q$ is the best choice of $v p$, because as for sum function this point is the one in data space that minimizes the value of aggregate distance. We can say that the aggregate nearest neighbor is a point of P which 'near' the aggregate centroid of Q . However it is difficult and time-consuming to calculate the aggregate centroid. Thus we use the geometric centroid to substitute it. The geometric centroid: $\mathrm{q}(\mathrm{x}, \mathrm{y})$ of Q can be calculated by Eq. 1 and Eq.2.

$$
\begin{align*}
& x=(1 / n) \cdot \sum_{i=1 . . n} x_{i}  \tag{1}\\
& y=(1 / n) \cdot \sum_{i=1 . . n} y_{i} . \tag{2}
\end{align*}
$$

Although the geometric centroid of query points set Q is the best choice of $v p$, it is not certain a point of the dataset $P$. if we choose it as vp , it is possible that the search region R would be a empty set. For the reason we find the nearest neighbor of the geometric centriod in P (Assuming this point is $\mathrm{p}_{\mathrm{k}}$ ), and choose $\operatorname{it}\left(\mathrm{p}_{\mathrm{k}}\right)$ as the vp point instead of the geometric centriod. On this vp, there is at least one point $p_{k}$ in the search region $R$. For the search region always covers the MBR of query points set, vp-ANN algorithm is strong and always can get the best ANN query point.

### 2.2 Projection-based Algorithm

The heart of the projection-based method is to project the query points into a carefully selected 'line'. The projecting result can reflect the distributing of query points. By the distributing of the projecting points in the line we can determine the search region in which the query points distribute concentrated, and prune other region. The search region of projection-based algorithm is the intersection of two candidate regions. The candidate region is a cirque between the two circles. Both of the candidate regions contain all the query points.
In order to calculate the candidate region, projection-based method chooses two points $p_{a}$ and $p_{b}$ in data set $P$, and considers the 'line' that passes through $\mathrm{p}_{\mathrm{a}}$ and $\mathrm{p}_{\mathrm{b}}$ in data space, then projects the query points into the line. The distances between pivot $p_{a}$ and the projecting points of the query points on the line can be calculated by the Eq.3, which can be deduced by cosine law. In the equation $\mathrm{D}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}\right)$ is the Euclidean distance between $\mathrm{p}_{\mathrm{a}}$ and q . In order to let our algorithm be more strong, the points $p_{a}$ and $p_{b}$ we select should maximize the distance $D\left(p_{a}, p_{b}\right)$. This means $p_{a}$ and $p_{b}$ must be in the brim of data space. We choose this two
pivots by special method which requires just $O(N)$ distance computations.

$$
\begin{equation*}
\operatorname{Proj}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}\right)=\left(\mathrm{D}^{2}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}\right)+\mathrm{D}^{2}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{p}_{\mathrm{b}}\right)-\mathrm{D}^{2}\left(\mathrm{p}_{\mathrm{b}}, \mathrm{q}\right)\right) /\left(2 \mathrm{D}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{p}_{\mathrm{b}}\right)\right) \tag{3}
\end{equation*}
$$

After calculating all the value of $\operatorname{proj}\left(p_{a}, q_{i}\right)(i=1 . . n)$, we find out the query point $q_{\max }$ and $q_{\min }$, which the value of $\operatorname{proj}\left(p_{a}, q_{\max }\right)$ and $\operatorname{proj}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}_{\text {min }}\right)$ are the maximum and minimum respectively in $\operatorname{proj}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}_{\mathrm{i}}\right)(\mathrm{i}=1 . . \mathrm{n})$. Let $\mathrm{q}_{\max }$ ' be the projecting point of $\mathrm{q}_{\max }$ on the line and $\mathrm{q}_{\text {min }}{ }^{\prime}$ be the projecting point of $\mathrm{q}_{\min }$ on the line. For insuring that the candidate region would cover all the query points we calculate the radii of the candidate region by Eq. 4 and Eq. 5 .

$$
\begin{align*}
& \mathrm{r}_{\max }=\operatorname{proj}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}_{\max }\right)+\mathrm{D}\left(\mathrm{q}_{\max }, \mathrm{q}_{\max }{ }^{\prime}\right)  \tag{4}\\
& \mathrm{r}_{\min }=\operatorname{proj}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{q}_{\min }\right)-\mathrm{D}\left(\mathrm{q}_{\min }, \mathrm{q}_{\min }^{\prime}\right) \tag{5}
\end{align*}
$$

In Eq. 5 if $r_{\text {min }}<0$, we let $r_{\text {min }}=0$. Taking $p_{a}$ as the centre of a circle we draw two circles with the radii $r_{\text {max }}$ and $r_{\text {min }}$ respectively, the cirque between the two circles is the candidate region of projection-based method. We can express the candidate region by $\mathrm{A}\left(\mathrm{p}_{\mathrm{a}}, \mathrm{r}_{\text {min }}, \mathrm{r}_{\text {max }}\right)=\left\{\mathrm{p}\left|\mathrm{p} \in \mathrm{P}, \mathrm{r}_{\text {min }}<=\left|\mathrm{p}_{\mathrm{a}} \mathrm{p}\right|<=\mathrm{r}_{\max }\right\}\right.$.
Because the candidate region covers all the query points, it is certainly to cover the MBR of all the query points. Therefore this region is also a strong one and would include the best ANN point. However the range of the candidate region is still large, and it may include almost of the points in dataset. If we take this candidate region as search region, we just can prune a few points in data space. For get the search region which is much smaller than the candidate region, our strategy is: firstly, we select two points $p_{a 1}$ and $\mathrm{p}_{\mathrm{b} 1}$, and get the frist candidate region: $\mathrm{A}\left(\mathrm{p}_{\mathrm{a} 1}, \mathrm{r}_{\text {min } 1}, \mathrm{r}_{\text {max }}\right)$. Then we select the other two points $p_{a 2}$ and $p_{b 2}$ which are different from $\mathrm{p}_{\mathrm{a} 1}$ and $\mathrm{p}_{\mathrm{b} 1}$, and get the second candidate region $\mathrm{A}\left(\mathrm{p}_{\mathrm{a} 2}, \mathrm{r}_{\min 2}, \mathrm{r}_{\max 2}\right)$. Because the two region have different circle centres $\mathrm{p}_{\mathrm{a} 1}$ and $\mathrm{p}_{\mathrm{a} 2}$, and we project just the same dataset P into the two different lines, there must be an intersecting region between $\mathrm{A}\left(\mathrm{p}_{\mathrm{a} 1}, \mathrm{r}_{\text {min1 }}, \mathrm{r}_{\text {max1 }}\right)$ and $\mathrm{A}\left(\mathrm{p}_{\mathrm{a} 2}, \mathrm{r}_{\text {min } 2}, \mathrm{r}_{\text {max } 2}\right)$. This intersecting region would much smaller than each one of the two candidate regions, and We symbolize this region by $\mathrm{S}=\mathrm{A}\left(\mathrm{p}_{\mathrm{a} 1}, \mathrm{r}_{\min 1}, \mathrm{r}_{\text {max }}\right) \cap \mathrm{A}\left(\mathrm{p}_{\mathrm{a} 2}, \mathrm{r}_{\text {min } 2}, \mathrm{r}_{\text {max } 2}\right)$. We select S as the search region of projection-based algorithm. Because both the two candidate regions cover the MBR of the query points, this search region is a "satisfied" one.

## 3. EXPERIMENTS

We use both real datasets and synthetic datasets in our experiments. The result shows that the value of $n$ (point number of Q) and the area of MBR of Q are the important factors of our algorithms. And as for CPU cost, the projection-based algorithm is better than vp-ANN algorithm. Our methods perform well in high dimension space.

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