

# *A Fair Cloud Resource Allocation using Data Envelopment Analysis*

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**Abstract**—Internet technology is advancing with each passing day, the user's demand is also increasing. Of course the users will more concern to quality of service. The vendors must find out a win win method of resource allocation to meet users and itself. Therefore, the resource allocation of cloud computing has become one of hottest topics. In literatures, some researchers have proposed resource allocation methods which include allocation of virtual machines and service classification, etc. However, these methods are based on subjective observations that lead to the overall cloud architecture becomes imbalance. In order to prevent such situation happened, we use the Data Envelopment Analysis (DEA) to solve the imbalance problem. In this paper, our analysis is start from the user's requests, and use the DEA to evaluate the whole cloud parameters. Then we can find out the resource allocation policy which is the most suitable between the users and vendors.

**Keywords**- Cloud Computing; Resource Allocation; Data Envelopment Analysis.

## I. INTRODUCTION

Resource allocation is a very important issue in the cloud computing [1][2][3][4]. For providers, regardless of the issue exists in the infrastructure, service and platform, all of the solution also want to achieve a balanced system [5] with high quality service [6] and less bandwidth [13]. In general, some methods solve this problem by the VM adjustment, because the VM has a high relationship with the any services and the users directly. They allocate the number of VM according to the user's requirements, CPU capacity or bandwidth. Briefly, to allocate the VM from the resource pool to users is a more simple and efficient approach that are shown in the figure 1.

The resource allocation problems are often involved to the trade-off design, because the influence of each parameter will be different when it is in the specific system and these trade-off relations are close. It represents that we cannot focus on a parameter only. Otherwise, If we still do that, the whole system may be imbalance.

Nowadays has a lot of researches investigate the cloud resource allocation issues. The research scope involves many different service types which include Software as a Service(SaaS), Platform as a Service(PaaS) and Infrastructure as a Service(IaaS). Whether which types about cloud resource allocation that are all in accordance with user requirements to allot datacenter's resources for users.

There are some of researches in cloud resource allocation that are dynamic allocation as well as providing optimal quality for service and minimize operating costs [1]. They focused on discussion of CPU resources usage, and they also used of Service Level Agreement(SLA) as resource allocation basis to protect the user perceived Quality of Service(QoS). However, these methods take into account only a few of target. In fact we cannot use only such parameters to completely describe the entire cloud environment. If we remain to run these methods, the cloud system will focus on the part of the operation only. In this way, some important parts may be sacrificed. For the principle of fairness, we boldly hypothesize that more factors should be considered. Therefore, we had to consider demands of any users at any time.

In the paper, we use Data Envelopment Analysis(DEA) to analyze resource allocation problem which include user's demand, distance, CPU utilization and cost, etc. DEA can

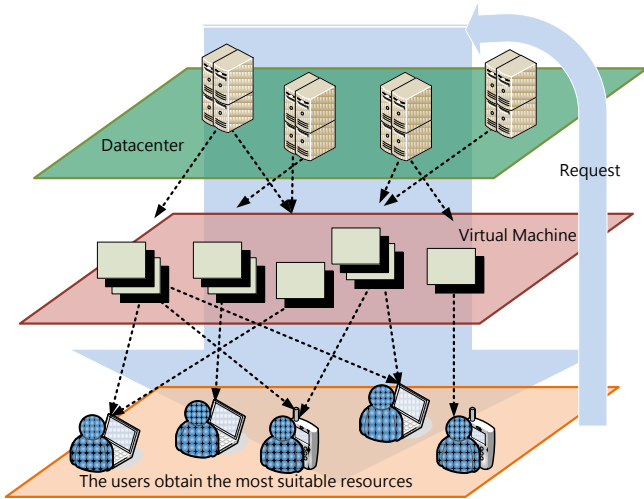


Figure 1. Cloud resource allocation diagram

analyze multi-output and multi-input simultaneously. It can show the relationship between each project according to the DEA characteristics which consider to the influence with each parameters. Finally, the analysis results will provide any users and service provider to find out the most appropriate resource allocation policy.

This paper is organized as follows: In section 2, we introduce some related works about cloud resource allocation problem. In section 3, we use DEA to find the optimal resource allocation policy. In section 4, we can evaluate the pros and cons of DEA. Finally we will summarize the contribution of this paper, and simply distribute the future works.

## II. BACKGROUND

### A. Cloud Resource Allocation

In [8], the authors minimize the execution time and to achieve the costs reduction. The authors also consider to total cost time includes Virtual Machines (VM) which is start, close or idle. Then use of these messages to reach resource allocation and configuration. In [9], the authors is to find out the datacenter which meets user's demand and it is closest to the user. The proposed algorithm determines remnants storage space of the datacenter whether meets the user's requirement then evaluates delay time from all datacenter's workload generation. By the results, the most suitable datacenter can be found. In [10], the authors address the load balance problem which generate from the unexpected requirements. Such requirements will make the performance decreasing. The proposed method use the greedy principle in minimal load to make datacenter selection. Even though these papers discussed the cloud resource allocation, but the impact parameters are not only one. Most previous studies are consider a few factors only, cause the results are subjective. Therefore, we should consider to more factors as far as possible to satisfy whether users or suppliers.

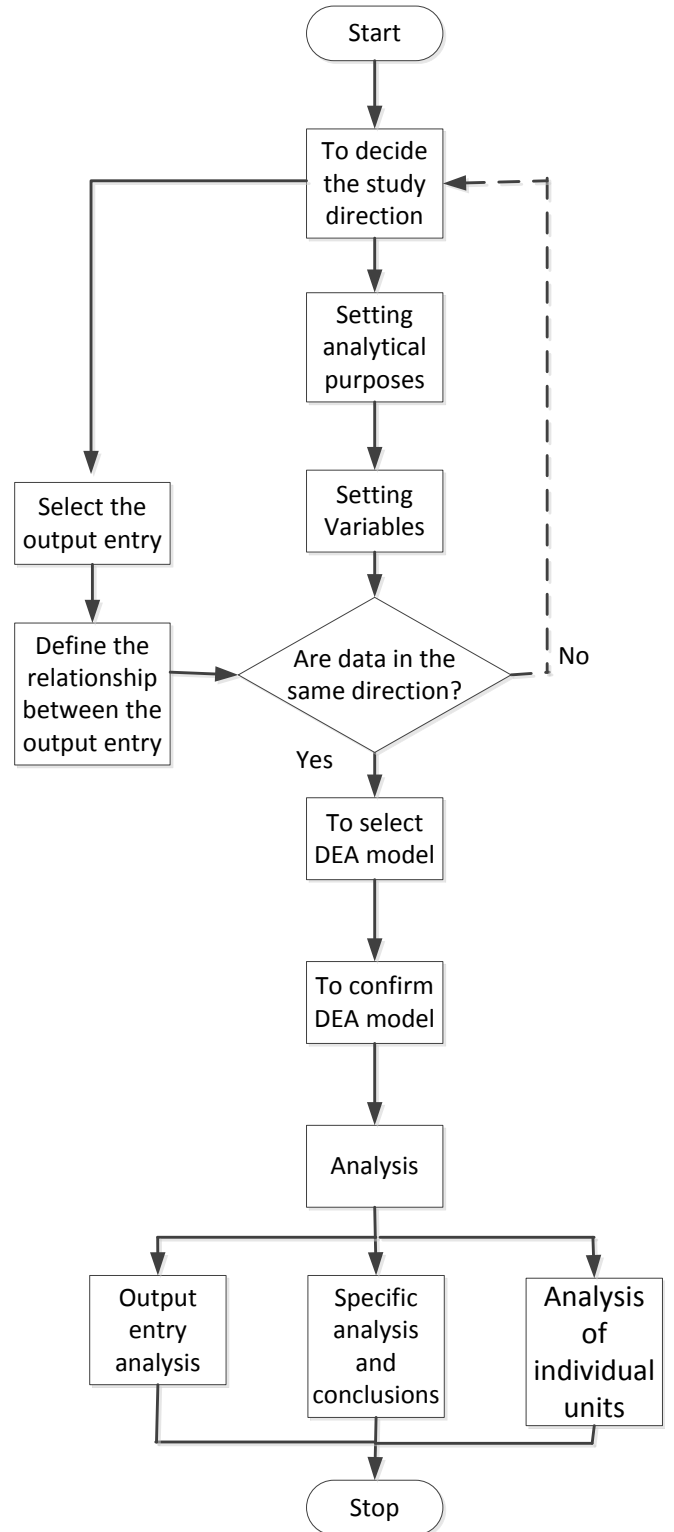


Figure 2. Workflow of DEA

### B. Data Envelopment Analysis

Data Envelopment Analysis(DEA) is a Pareto optimality according to some researches analysis of economics. The evaluating out most favorable result is assessed under efficiency value is the objective environment. DEA is a multi-output and multi-input analysis policy. Therefore, the conditions will be a relative target for other units so that they will not only mutual consideration but also the analyzed results will make each parameters accept. In simple term, this mathematical model hammer out the relative efficiency decision making any units be enveloped. The analyzed items must have homogeneity, hence we need to add Zweights so that the parameters can be pulled together to look at the same level. And this method use DMU curve to determine the smaller gap to closer the optimal solution [11][12].

A simple example, a basketball team manager can use DEA to allocate payroll. Usually a basketball team have limited total salary expenditure. How to allocate these salaries to the players for the fairest without waste? It is a very important issue for the team manager. At this time use the most convincing performance of each player as the metrics for DEA. These metrics include three-point shooting, rebounding, assists and blocked shots, etc. And we can observe that each parameter influence for the basketball game. Finally, the highest performance one can get the highest salary, thus every penny can be spent valuable do not wronged.

Figure 2. is DEA of flow chart. We determine our research direction of cloud resource allocation firstly, then we set the analysis goal to meet user's requirement for with principles of fairness. Next we decide input/output definition. Finally, we can determine DEA mode and analyzing.

### III. ALLOCATION PROBLEM AND POLICY

In order to design a fair resource allocation in cloud environment, we use DEA to do the analysis on various factors. We chose DEA be our analysis tool because it consider many factors in simultaneously as well as every factors interaction. In this way, we just find out the optimal solution in various cases. Such interaction is usually exist in the resource allocation problem that there are two or more factors will affect in a same target or affect with each others. For a instance, the user will be a preferred if he is closer to the datacenter. It represents that the other users just the second choice for the datacenter. It shows the interaction of distance may has the influence for the user 's use rights. For another example, there are three users send the request to datacenter. In this time, the datacenter may provides a great resource to first user so that the others just send the request for the remaining resources in datacenter. In shows the interaction of order may has the influence for the user 's use rights. Therefore, we must taking into account to any user's characteristics such as distance, load and CPU utilization, etc. Because, any resources are datacenter's limited assets so that it simply cannot meet all the requirements. In order to achieve the fair allocation, the weights definition is a very important step so that they will be set to the same level can be compared. Before the weights design, we introduce the symbols which will be used in next subsection.

### A. Symbols and Definitions

Formula (1) is the evaluated units of user in DEA :

$$User_k, k = 1, 2, 3, \dots, n. \quad (1)$$

Input data includes Demand, Cost, Utilization and Performance. Demand means the capacity of VM user needs. Cost means how much money to rent the resource. Utilization means how much capacity of datacenter which have rented to user. Performance means performance of requirements user wants.

TABLE I. SYMBOLS DEFINITION OF INPUT DATA

| INPUT       |         |
|-------------|---------|
| Demand      | $irq_k$ |
| Cost        | $ic_k$  |
| Utilization | $iu_k$  |
| Performance | $ip_k$  |

Output data includes Resource, Cost, Utilization, Performance, Workload, Distance, Wasting time, Capacity and Idle. Resource means resource from datacenter that can provide to the user. Cost means datacenter running cost. Utilization and Workload means utilization and workload of datacenter. Distance means transmission delay generated from that the distance between the datacenter and the user. Wasting time means average time by VM on/off. Capacity means remaining available resources. Idle means the average time spent when VM has done the task but it do not shut down.

TABLE II. SYMBOLS DEFINITION OF OUTPUT DATA

| OUTPUT       |         |
|--------------|---------|
| Resource     | $ore_k$ |
| Cost         | $oc_k$  |
| Utilization  | $ou_k$  |
| Performance  | $op_k$  |
| Workload     | $ow_k$  |
| Distance     | $od_k$  |
| Wasting time | $owt_k$ |
| Capacity     | $oca_k$ |
| Idle         | $oid_k$ |

DEA limits the sum of weights as 1 as well as let the weight generated by mathematical programming so that there are not artificially subjective view points. Therefore, use of DEA can meet the principle of fairness.

TABLE III. SYMBOLS DEFINITION OF USERS (USER NUMBER 1~K)

|          |       |
|----------|-------|
| $User_1$ | $w_1$ |
| $User_2$ | $w_2$ |
| $User_3$ | $w_3$ |
| $User_k$ | $w_k$ |

TABLE IV. OUTPUT ITEM

| INPUT       | $User_1$ | $User_2$ | $User_3$ | UNIT             |
|-------------|----------|----------|----------|------------------|
| Demand      | 4.00     | 16.00    | 8.00     | Gb               |
| Cost        | 1.00     | 5.00     | 2.55     | Thousand dollars |
| Utilization | 90.00    | 50.00    | 70.00    | %                |
| Performance | 2.00     | 1.00     | 3.00     | Demand /Sec      |

TABLE V. INPUT ITEM

| OUTPUT       | $User_1$ | $User_2$ | $User_3$ | UNIT             |
|--------------|----------|----------|----------|------------------|
| Resource     | 1024     | 1024     | 1024     | Tb               |
| Cost         | 1.20     | 1.20     | 1.20     | Thousand dollars |
| Utilization  | 40.00    | 40.00    | 40.00    | %                |
| Performance  | 6.00     | 6.00     | 6.00     | Demand /Sec      |
| Workload     | 20.00    | 20.00    | 20.00    | %                |
| Distance     | 10.00    | 25.50    | 35.00    | Kilometer        |
| Wasting time | 5.00     | 5.00     | 5.00     | Sec              |
| Capacity     | 2048     | 2048     | 2048     | Gb               |
| Idle         | 2.00     | 2.00     | 2.00     | Sec              |

### B. Limitation

Here we make an example with  $User_1$ . Based on a fair principle of resource allocation, we must minimize the efficiency indicators be a reference to allocate the resources since resource of datacenter is limited.  $E$  is means efficiency indicators. It used to decide that the resource from the datacenter user can uses.

$$\text{Minimize } E. \quad (2)$$

The used weight of DEA evaluate efficiency which must be a most favorable weight for evaluation units. DEA limit weight of sum must be 1 as following:

$$w_1 + w_2 + w_3 + \dots + w_k = 1. \quad (3)$$

The constraint formula of input gets weight of all users from output constraint formula firstly. Next, the efficiency indicator is calculated from the input formula. For each input, we have to provide a constraint let the input of datacenter is equal or lesser than Resource of datacenter:

$$\text{Input of Datacenter} \leq \text{Resource of datacenter}. \quad (4)$$

Input value:

$$\begin{aligned} (\text{Input item of datacenter}) &= (User_1) \times w_1 + \\ & (User_2) \times w_2 + \dots + (User_k) \times w_k. \end{aligned} \quad (5)$$

An example by Demand:

$$\begin{aligned} (\text{Demand}) &= (User_1) \times w_1 + \\ & (User_2) \times w_2 + \dots + (User_k) \times w_k. \end{aligned} \quad (6)$$

Total input item:

$$w_1 irq_1 + w_2 irq_2 + \dots + w_k irq_k \leq irq_1 E. \quad (7)$$

$$w_1 ic_1 + w_2 ic_2 + \dots + w_k ic_k \leq ic_1 E. \quad (8)$$

$$w_1 iu_1 + w_2 iu_2 + \dots + w_k iu_k \leq iu_1 E. \quad (9)$$

$$w_1 ip_1 + w_2 ip_2 + \dots + w_k ip_k \leq ip_1 E. \quad (10)$$

T Output constraints must provide a set of weight so that each output are equal or greater than output of users. For each output, we must provide a constraints formula to claim output of datacenter are equal or greater than evaluated users:

$$\text{Output of Datacenter} \geq \text{Evaluated user}. \quad (11)$$

Input value:

$$\begin{aligned} (\text{Onput item of data center}) &= (User_1) \times w_1 + \\ & (User_2) \times w_2 + \dots + (User_k) \times w_k. \end{aligned} \quad (12)$$

An example by Demand:

$$\begin{aligned} (\text{Resource}) &= (User_1) \times w_1 + \\ & (User_2) \times w_2 + \dots + (User_k) \times w_k. \end{aligned} \quad (13)$$

Total input item:

$$w_1 ore_1 + w_2 ore_2 + \dots + w_k ore_k \geq ore_1. \quad (14)$$

$$w_1 oc_1 + w_2 oc_2 + \dots + w_k oc_k \geq oc_1. \quad (15)$$

$$w_1 ou_1 + w_2 ou_2 + \dots + w_k ou_k \geq oc_1. \quad (16)$$

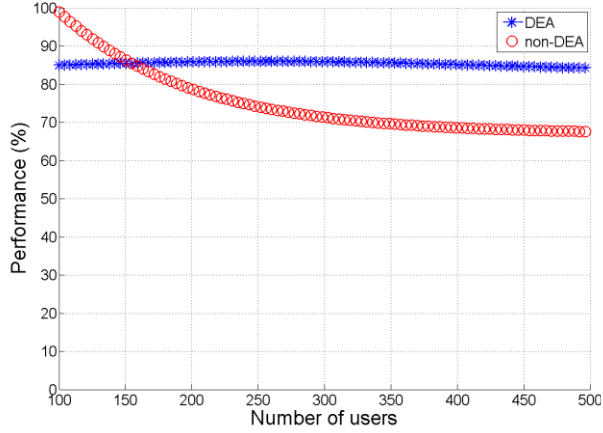


Figure 3. Performance Comparison

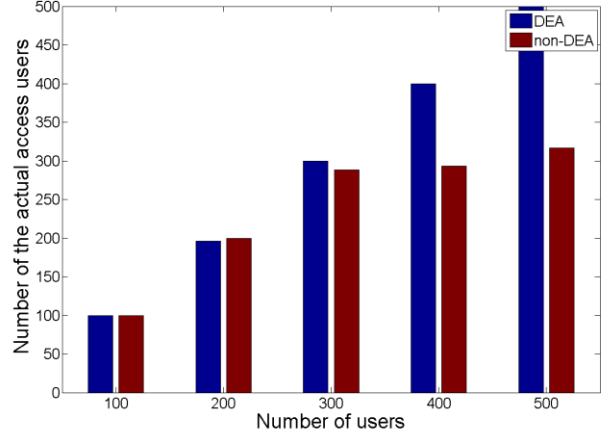


Figure 4. The number of users actually used the cloud system

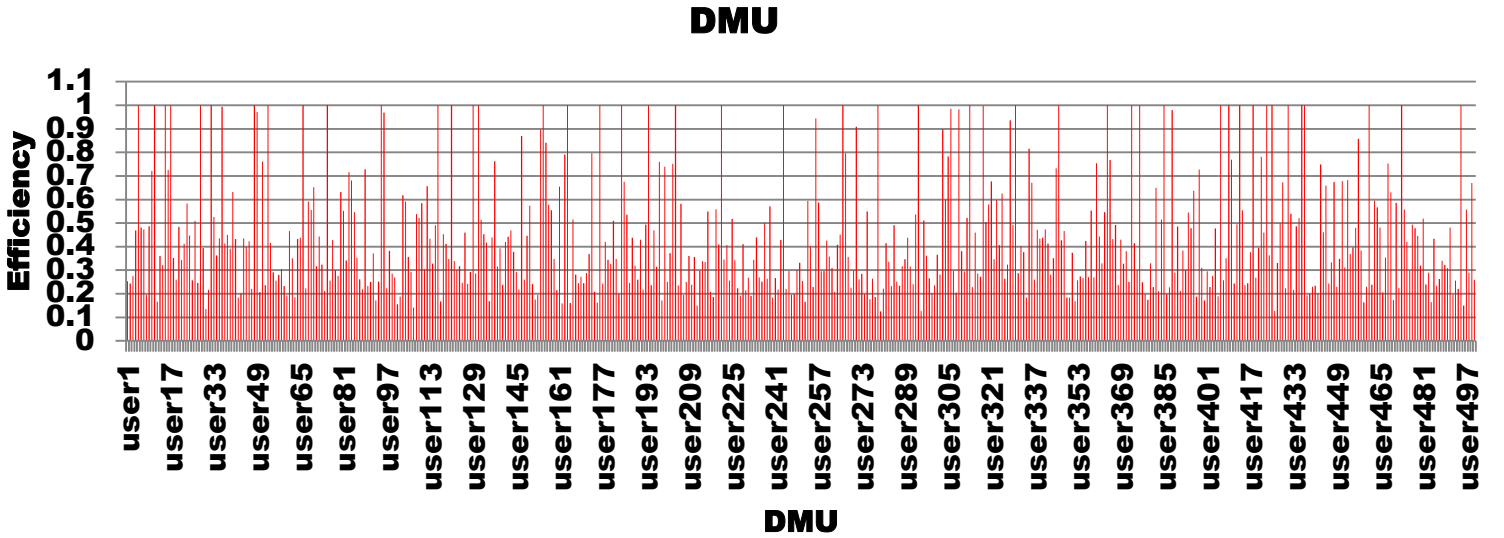


Figure 5. Users phenomenon of dynamic access

$$w_1op_1 + w_2op_2 + \dots + w_kop_k \geq op_1. \quad (17)$$

$$w_1ow_1 + w_2ow_2 + \dots + w_kow_k \geq ow_1. \quad (18)$$

$$w_1od_1 + w_2od_2 + \dots + w_kod_k \geq od_1. \quad (19)$$

$$w_1owt_1 + w_2owt_2 + \dots + w_kowt_k \geq owt_1. \quad (20)$$

$$w_1oca_1 + w_2oca_2 + \dots + w_koca_k \geq oca_1. \quad (21)$$

$$w_1oid_1 + w_2oid_2 + \dots + w_koid_k \geq oid_1. \quad (22)$$

Decision variables

$$E, w_1, w_2, w_3, \dots, w_k \geq 0. \quad (23)$$

#### IV. EVALUATION

We use DEA-SOLVER Pro5.0 be our evaluation tool [14]. We assume our system environment that there are three users send the requirements to a same datacenter. Table 4 shows the list of detail of users proposed requirements. And the Table 5 list the state of resource in datacenter.

If  $E = 1$ , the user gets requirement 4.00. If  $E > 1$ , the user gets requirement greater than 4.00. If  $E < 1$ , the user gets requirement less than 4.00.

DEA has two characteristics:

- Decision variable  $(E, w_1, w_2, w_3)$  has at least one solution.
- By characteristics 1, we know  $(E, w_1, w_2, w_3)$  has one solution can mapping to  $E = 1$ , and  $E \geq 0$  so that Minimal E will place between 0 and 1.

Figure 3 shows that the relationship between the number of users and performance. In less users case, the non-DEA allocation policy approaches to greedy way. The first user will gets the resource as much as possible. In other words, the datacenter may allocates the resource that based on the upper-bound of first user's requirements if there are enough resources in the resource pool. Late users may lose some opportunities to get more resources. DEA solves this problem through more user information comparison in addition to the only one user case. When the number of users increasing, DEA can consider to more interaction so that the performance of DEA will be relatively stable.

Figure 4 shows that the number of users actually used the cloud system. When number of users are 100 and 200, DEA and non-DEA can average allocate resource to the users since the resources in resource pool are enough. But in 300 or more users case, non-DEA let some users cannot get resource because the resource pool have be filled from the previously several users. However, we can make more precise analysis by DEA. Therefore, we can see that the gap between the DEA line and non-DEA line is Increasing by the growing user number.

Figure 5 shows that the efficiency for every users. Here we give DMU with 500 users randomly. In order to show a dynamic scenario, we let users can freely access the datacenter. Sometimes the efficiency usually between 20% to 60%. Because it is a dynamic behavior of the user's access so that the DEA must continually recalculate. However we can see that some time slot still maintained 100% efficiency. It represents that DEA still has the ability to instantly corrected.

## V. CONCLUSION AND DISCUSSION

We use DEA to analyze the various parameters in the cloud resource allocation problem. It can summarize to the most appropriate resource allocation policy so that this cloud system achieve impartial without imbalance. However, this way is too perfect that must used to a running system with several users. It represents that it ignored the initial condition only. But we can still see it as one of the best indicators according to Pareto optimality feature of DEA. In our future work, we will design a more flexible scheme to complete the DEA method as well as approaching the best possible condition from mere DEA.

## ACKNOWLEDGMENT

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