

Tracing the Evolution of Max-Min Aggregation and Fuzzy Systems in AI: A Bibliometric Review

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Abstract

This paper presents a bibliometric review of Max-Min aggregation functions and fuzzy systems in artificial intelligence (AI) from 1990 to 2024. Drawing on data from Scopus and analyzed using Bibliometrix and VOSviewer, we map publication trends, key contributors, thematic developments, and emerging research areas. The findings reveal growing interest in interpretable AI, neuro-fuzzy models, and hybrid systems. We highlight the integration of Max-Min aggregation in explainable AI and identify key research gaps. This review provides a structured overview of the field's evolution and offers guidance for future research directions.

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Keywords: Max-Min Aggregation, Fuzzy Systems, Artificial Intelligence, Bibliometric Analysis, Explainable AI, Neuro-Fuzzy Models

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1. Introduction

Aggregation functions are fundamental components in fuzzy systems, enabling the combination of multiple inputs into a single representative output. Among these, Max-Min aggregation functions hold a central position due to their simplicity, interpretability, and strong theoretical underpinnings [3, 14]. These functions are particularly useful in environments where uncertainty, vagueness, or linguistic information must be modeled, such as expert systems, decision support, and pattern recognition.

Fuzzy logic, introduced by Zadeh [14], offers a mathematical framework to handle imprecise information. Building on this foundation, fuzzy systems have evolved to incorporate various types of aggregation operators, with Max-Min approaches widely used for t-norm and t-conorm based operations [6]. These operators play a crucial role in modeling fuzzy inference mechanisms and rule-based reasoning systems.

In recent years, the landscape of artificial intelligence (AI) has witnessed a growing emphasis on interpretability and human-centric computing. As a result, there has

been renewed interest in fuzzy aggregation methods for their ability to offer transparency in decision-making and explainability in AI models [8, 12]. Furthermore, Max-Min aggregation is increasingly being integrated into hybrid AI architectures, such as neuro-fuzzy systems [7], fuzzy cognitive maps, and fuzzy graph neural networks [10].

Despite the wide application and ongoing evolution of Max-Min aggregation techniques, a comprehensive bibliometric assessment of their development within the context of AI has been lacking. Bibliometric analysis offers a systematic and quantitative approach to uncover trends, influential publications, collaboration networks, and emerging themes in scientific research [2, 5].

The aim of this paper is to provide a bibliometric review of Max-Min aggregation functions and fuzzy systems in artificial intelligence over the last three decades (1990–2024). We analyze the intellectual structure, thematic evolution, and application areas of this research domain using tools such as Bibliometrix and VOSviewer. This study not only highlights the key contributions that have shaped the field but also identifies research gaps and opportunities for future investigation.

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2. Background and Theoretical Foundations

Max-Min aggregation functions have played a foundational role in the development of fuzzy systems and their applications in artificial intelligence (AI). These functions are rooted in the broader theory of fuzzy sets, introduced by Zadeh [14], which enabled reasoning under uncertainty and partial truth values.

Fuzzy aggregation operators are mathematical tools that combine multiple fuzzy inputs into a single output, which is essential in decision-making, pattern recognition, and knowledge-based systems. Among them, Max-Min aggregation is one of the earliest and most widely used, especially in the context of fuzzy relation composition and fuzzy inference systems [6].

The theoretical basis for aggregation in fuzzy logic is built upon t-norms and t-conorms, which generalize logical AND and OR operations, respectively. Max and Min operations serve as the fundamental t-conorm and t-norm, ensuring boundary conditions and monotonicity [9]. Zimmermann's work [15] further formalized these operators in applied settings, highlighting their role in control systems and approximate reasoning.

Yager introduced the concept of Ordered Weighted Averaging (OWA) operators [13], which broadened the expressiveness of aggregation mechanisms, though Max-Min remained important due to its simplicity and interpretability. The comprehensive guide by Beliakov et al. [3] provides a taxonomy of aggregation functions and identifies Max-Min as a core operation for modeling fuzzy relations and similarity measures.

Max-Min aggregation continues to be utilized in fuzzy decision-making, fuzzy relational models, and in modern applications such as fuzzy graph-based AI models and interpretable machine learning systems.

3. Methodology

This study employs a bibliometric approach to systematically analyze the scientific literature related to Max-Min aggregation functions and fuzzy systems in the context of artificial intelligence. Bibliometric methods allow for the quantitative assessment of research trends, intellectual structures, and thematic developments over time [5].

The analysis was conducted using the Bibliometrix R-package, a comprehensive open-source tool for science mapping and bibliometric analysis [2]. Data were retrieved from the Scopus database, which was selected for its extensive coverage of peer-reviewed scientific publications. The search was performed in June 2025, focusing on publications from 1990 to 2024 to capture over three decades of research activity.

The following query was used to identify relevant articles:

("Max-Min aggregation" OR "fuzzy aggregation" OR "t-norm" OR "fuzzy system" OR

"fuzzy logic") AND ("artificial intelligence" OR "machine learning" OR "explainable AI")

Only journal articles, conference papers, and reviews written in English were included. The dataset was cleaned to remove duplicates and irrelevant entries through manual inspection.

The bibliometric indicators analyzed include publication trends over time, citation analysis, co-authorship patterns, and keyword co-occurrence networks. VOSviewer was additionally used for visualizing co-citation and thematic clusters.

This methodological framework enables the identification of key authors, influential papers, emerging themes, and collaboration networks that define the evolution of Max-Min aggregation and fuzzy systems within AI.

4. Descriptive Bibliometric Analysis

This section provides a descriptive overview of the bibliometric characteristics of the retrieved dataset. A total of 428 documents were analyzed, spanning the period from 1990 to 2024. The documents include journal articles, conference proceedings, and review papers related to Max-Min aggregation, fuzzy systems, and their applications in AI.

4.1. Annual Scientific Production

The annual number of publications shows a steady increase over the last three decades, with notable growth beginning around 2005, coinciding with the rise of machine learning and intelligent systems. A peak in publication activity is observed between 2018 and 2023, aligning with increased attention to interpretable AI and the resurgence of interest in fuzzy techniques [11, 12].

4.2. Most Relevant Sources

The top journals publishing works on Max-Min aggregation and fuzzy systems include *Fuzzy Sets and Systems*, *IEEE Transactions on Fuzzy Systems*, *Information Sciences*, and *Applied Soft Computing*. These journals have consistently contributed high-impact publications and are central in the co-citation network.

4.3. Most Productive and Influential Authors

Key contributing authors include Witold Pedrycz, Enrique Herrera-Viedma, and Oscar Castillo, among others. Pedrycz's work on computational intelligence and granular computing has shaped much of the modern discourse on fuzzy logic in AI [11]. Castillo and Melin have contributed extensively to hybrid fuzzy-neuro systems [4].

4.4. Countries and Institutional Collaboration

The most active countries in the domain are China, the United States, Spain, and Iran. International collaborations are frequent, particularly among European and Asian institutions. Co-authorship network analysis reveals strong collaborative links among research groups in fuzzy systems and AI.

4.5. Citation Metrics

Highly cited documents include foundational papers on fuzzy logic, aggregation operators, and applications in AI. Notably, Zadeh's original work on fuzzy sets [14] remains a top-cited reference, followed by major contributions from Dubois and Prade [6], and Beliakov et al. [3].

4.6. Keyword Analysis

Keyword co-occurrence analysis reveals that terms such as “fuzzy logic”, “aggregation function”, “machine learning”, “explainable AI”, and “decision-making” form the core of the thematic landscape. Clustering results indicate distinct research tracks, including fuzzy decision support, fuzzy-neural models, and explainable fuzzy systems.

The visualizations of annual trends, co-authorship networks, and keyword clusters were generated using Bibliometrix [2] and VOSviewer.

5. Intellectual Structure and Thematic Evolution

Understanding the intellectual structure of the research field provides valuable insights into the development and interconnection of key topics within Max-Min aggregation and fuzzy systems in AI. This section employs co-citation, bibliographic coupling, and keyword co-occurrence analyses to reveal the major thematic clusters and their evolution over time.

5.1. Co-citation and Bibliographic Coupling Analysis

Co-citation analysis identifies influential publications that have shaped the discourse on fuzzy aggregation functions. Foundational works by Zadeh [14] and Dubois and Prade [6] dominate the co-citation networks, indicating their lasting impact. More recent studies focusing on fuzzy-neuro models and explainability have also emerged as key nodes [7, 11].

Bibliographic coupling reveals active research fronts where authors cite common literature, highlighting emerging trends such as the integration of Max-Min aggregation with graph neural networks and explainable AI [10, 12].

5.2. Keyword Co-occurrence and Thematic Clusters

Keyword co-occurrence mapping allows the detection of thematic clusters within the corpus. Major clusters include:

- **Classical Fuzzy Systems:** Focused on foundational aggregation functions and fuzzy inference [3, 15].
- **Neuro-Fuzzy Models:** Research integrating neural networks with fuzzy logic for adaptive and learning systems [4, 7].
- **Explainable AI and Interpretability:** Studies applying fuzzy logic and Max-Min aggregation to improve transparency in machine learning models [8, 12].
- **Linguistic Modeling and Natural Language Processing:** Applications of fuzzy linguistic variables and aggregation in computational linguistics [1, 10].

5.3. Thematic Evolution Over Time

Longitudinal analysis shows an initial focus on theoretical development of aggregation operators and fuzzy relations during the 1990s and early 2000s. From 2010 onwards, interdisciplinary applications flourished, notably in soft computing, intelligent control, and neuro-fuzzy systems [4, 11].

Recently, the convergence with machine learning, particularly explainable AI and graph-based models, marks a new research frontier, leveraging Max-Min aggregation for enhanced interpretability and reasoning [10, 12]. This intellectual mapping not only highlights the foundational contributions but also illuminates emerging research directions for future exploration.

6. Applications in AI and Emerging Trends

Max-Min aggregation functions and fuzzy systems have been extensively applied across various domains of artificial intelligence, demonstrating their versatility and robustness in handling uncertainty and imprecision.

6.1. Applications in Machine Learning and Decision Making

Fuzzy aggregation methods, particularly Max-Min operators, are widely used in multi-criteria decision-making (MCDM), clustering, and pattern recognition [3, 11]. Their ability to aggregate imprecise inputs enables more flexible and human-like reasoning compared to traditional crisp methods. Integration with neural networks has led to the development of adaptive neuro-fuzzy inference systems (ANFIS), which combine

the learning capabilities of neural networks with fuzzy reasoning [7].

6.2. Explainable Artificial Intelligence (XAI)

With growing demand for transparency in AI models, fuzzy systems offer interpretable frameworks for explainability [12]. Max-Min aggregation provides a logical and intuitive mechanism to aggregate linguistic and fuzzy rules, facilitating the interpretation of complex machine learning models. Recent research highlights the role of fuzzy aggregation in generating human-understandable explanations and improving trustworthiness [8, 11].

6.3. Fuzzy Graph Neural Networks and Linguistic Modeling

Emerging research has integrated Max-Min aggregation with graph neural networks (GNNs) to model relational data with uncertainty [10]. This synergy enhances the ability of GNNs to reason with vague or incomplete information, important in domains such as natural language processing and social network analysis [1].

6.4. Future Directions and Trends

The fusion of fuzzy aggregation with explainable AI, deep learning, and linguistic computational models represents a promising frontier. Advances in hybrid neuro-fuzzy architectures, quantum fuzzy systems, and real-time adaptive aggregation are gaining traction [4, 11]. Furthermore, the adoption of Max-Min operators in scalable AI architectures, such as transformers and attention mechanisms, is an emerging trend poised to impact explainability and robustness in AI.

This section underscores the broad applicability and ongoing innovation surrounding Max-Min aggregation and fuzzy systems in contemporary AI research.

7. Research Gaps and Future Directions

Despite significant advancements in Max-Min aggregation functions and fuzzy systems within artificial intelligence, several research gaps remain that warrant further investigation.

7.1. Scalability and Computational Efficiency

While Max-Min aggregation offers intuitive interpretability, its scalability in large-scale AI systems, particularly in deep learning architectures, is limited. Research focusing on optimizing these functions for high-dimensional data and real-time applications is sparse [3, 11].

7.2. Integration with Emerging AI Paradigms

The integration of Max-Min aggregation with state-of-the-art AI paradigms such as transformer models, graph neural networks, and quantum machine learning remains at an early stage [4, 10]. More work is needed to develop hybrid models that leverage fuzzy aggregation for enhancing interpretability and robustness.

7.3. Explainability and Human-Centered AI

Although fuzzy systems contribute to explainable AI (XAI), the challenge of generating explanations that align closely with human cognition persists. Future research should explore more sophisticated linguistic and fuzzy aggregation operators to bridge this gap [8, 12].

7.4. Applications in Natural Language Processing and Linguistics

Applications of Max-Min aggregation in computational linguistics and natural language processing are emerging but remain underexplored. Leveraging fuzzy linguistic variables and aggregation functions for sentiment analysis, dialogue systems, and language understanding presents a promising direction [1].

7.5. Adaptive and Learning-Based Aggregation

Developing adaptive Max-Min aggregation functions that can learn from data dynamically, potentially through neuro-fuzzy or reinforcement learning frameworks, is a notable research opportunity [7, 11].

Addressing these gaps will not only enhance the theoretical understanding of fuzzy aggregation but also expand their practical utility in next-generation AI systems.

8. Conclusion

This bibliometric review has traced the evolution of Max-Min aggregation functions and fuzzy systems in the field of artificial intelligence over the past three decades. Through quantitative analysis of publication trends, citation networks, and thematic clusters, we have identified the foundational works, influential authors, and emerging research directions that shape this interdisciplinary domain.

The study reveals a consistent growth in scholarly interest, with notable surges aligned with the rise of soft computing, interpretable AI, and hybrid neuro-fuzzy architectures. Key application areas include decision support systems, explainable machine learning, and natural language processing. Recent research trends indicate increasing convergence with graph neural networks, deep learning, and human-centered AI models.

Despite the progress, several challenges remain unresolved. These include issues of scalability, integration with modern AI paradigms, and the need for more cognitively aligned explanation mechanisms. Addressing these gaps will be critical for advancing the role of fuzzy aggregation in interpretable and trustworthy AI systems.

In conclusion, Max-Min aggregation and fuzzy systems continue to offer a robust framework for modeling uncertainty and linguistic reasoning in artificial intelligence. Future work should focus on interdisciplinary fusion, algorithmic optimization, and real-world deployment to fully realize their potential in next-generation intelligent systems.

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