A Life Extend Approach Based on Priority Queue N Strategy for Wireless Sensor Network

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Abstract

In this paper, we proposed a method on the tradeoff between packet transmission speed and battery life in wireless sensor networks (WSN). The data obtained by sensor nodes comprised various types of information with various levels of importance. A misjudgment of the priority of packets according to the importance of data may delay the transmission of important information. The energy consumed by sensor nodes varies according to system states. Therefore, this research used queuing theory and the birth-death process to build a mathematical model capable of quantifying various energy consumption parameters. MATLAB was used to calculate the distribution of system state probability for sensor nodes with two queues. Packet delay equation was then applied to obtain the expected values of delay time for packets of various priorities. We adjust various system parameters and observe how these changes influenced system state probability. Finally, we use different N values to obtain the minimal value of system energy consumption. Obtaining this value helps to overcome the energy hole problem (EHP), which in turn extends the lifespan of the overall WSN. Prioritizing packets can ensure the transmission of important data within a shorter time span. Experimental results show the energy consumption is reduced and important data can be transmitted with less packet delay time.

Keywords: WSN, EHP, Queuing Theory, Preemptive Priority Queue, Ubiquitous Sensor Networks

1. Introduction

The sensor nodes have been popularly used in the application of wireless sensor network (WSN). Mike first introduces the ubiquitous computing concept in 1991. The concept has been extensively used to increase the convenience of human life. The sensor node is becoming one key device to consist of the intelligent ubiquitous computing network (USN) such as medical monitoring, surveillance and tracking systems [1, 2]. Most of the USN is to collect and relay information to coordinator for integrating as useful knowledge [3, 4]. Each sensor may provide several different kind of information with different priority and importance. To ensure the important information can be transmitted in real-time manner, we schedule the information with different sequence based on its priority. Meanwhile, the network disconnection problem becomes more important when the scale of ubiquitous sensor network is increased. Most of the network disconnection problem is induced from the power consumption issues. Thus, the real-time and power consumption [5, 6] issues become a critical topic while considering to extending the lifetime and availability of ubiquitous computing network.

The energy consumption of sensor node is larger if the sensor node is near the sink node. This result in the energy hole problem (EHP) may happen [7]. The USN cannot work normally due to the network disconnection. According to the report of [8], there is 90 % energy left when the lifetime of WSN is ended. This is because there is more data packets to be relayed through these coordinate sensor nodes such that the energy consumption of coordinate sensor node is larger than other sensor node.

First Come First Service (FCFS) has been adopted in most USN applications. However, if there are some emergency data to be transmitted, the scenario might not be working properly. To resolve the EHP [9, 10, 11] and packet transmission real-time issues, we proposed a method based on threshold and priority queue to deal with the energy consumption and real-time transmission. This paper is arranged as follows. The second section discusses the related researches. The system infrastructure, analysis method, power consumption and the packet delay time are discussed in the third section. Experimental results are discussed in the fourth section. The fifth section is the conclusion.

2. Related Works

In [12], the average power demand of USN in sleep mode is 30mW and 80mW in transmission mode. Many researches [13,14] focus on the extension of life cycle in sleep mode. If the collision is happened, there is more power consumption in system [15]. The queue module of M/M/1/K is discussed in [16,17,18,19] to reduce the collision. These researches use single queue to save data packet and a threshold N as a basis to access the radio channel. When the number of packets in queue exceeds N, it tries to seize the channel for packet transmission.

The USN has to transmit data packet smoothly with considering to saving more power. USN does not transfer or receive any packet when it is in sleep mode. It only checks whether the incoming data packet is related to itself or not. If it's not in sleep mode when the related data packet is arrival, it is woken up from sleep mode [20, 21]. The process priority can be divided into non-preemptive priority and preemptive priority. Several researches [22,23,24,25] applied this approach on a queue structure buffer. The preemptive priority queue is favorable for higher priority packet by shortening the queuing time. In this paper, we proposed a method with dual queue priority structure to ensure the critical data packet can be handled in a more real-time manner with considering the extension of life cycle.

3. System Infrastructure 3.1 System Environment

In this research, we assume the transmission is in a half-duplex manner due to the concern of energy issue. Meanwhile, we set the queue size to be limited based on the realistic point of view. The system with four states, including Sleep State, Idle State, Busy State and Transmit State are also defined. The operation activities for each state can be shown in Figure 1. We define the priority level for each data queue to ensure critical information can be transmitted within a predicable period. To be more simplicity, we have illustrated a dual queue-based sensor node as an example. The high and low priority packets are named as n1 packet and n2 packet, separately. The high priority packet is stored in queue 1, and the low priority packet is in queue 2. The system is in sleep state at the initial phase of USN. There is no packet in the queue 1 and queue 2 at that time. The USN keeps stay at the sleep state and assigns n_1 and n_2 packets respectively to the queue 1 and queue 2. After that, the USN is wakeup and enters into the idle state. In idle state, the sensor node keeps continuing to receive the data packets until the number of packets in queue 1 and queue 2 is identical to N. Then, the USN changes to busy state.

When in busy state, the sensor node starts to access the radio channel. In general, the queue size is limited. We assume the queue size is K. The receiving activity of queue 1 and queue 2 will be stopped completely if the number of receiving data packets in queue 1 and queue 2 is equal to K. We assume n1 packet has higher priority than n2 packet. For the case of queue 1 is full and queue 2 is not full, if there is any n_1 packet arrived, the n_1 packet will be dropped. In contrast, the n₂ packet will be stored into the queue 2 buffer since the number of n₂ packet in queue 2 is still less than K. If the sensor node access the radio channel successful at busy state, it enters into the transmit state and doesn't receive any data packet. It transmits data packet in the queue until it is empty. The sensor node releases the access authority in case both queue 1 and queue 2 are empty. After that, it enters into the sleep state.



Figure 1: System operation flow

3.2 System Power Consumption

Generally, the number of packets in queue and transmission activity will affect the power consumption of sensor node. The power consumption in one cycle is shown in Figure 2, where the x and y axis denote the time and power consumption respectively. In the beginning, the sensor node stay at the sleep state and there is no packet accepted in the queue. The state changes to idle state if any data packet arrived. The power required at this period is called setup energy. The sensor node continues to accept the data packet such that it requires more energy to keep the increased data packet. Once the number of data packets in queue is equal to N, the state changes to busy. The sensor detects whether the radio channel is occupied by other nodes and gets the control authority of accessing radio channel. If the access is failed, it keeps staying at the idle state and continues to accept the data packet. These activities result in more energy needed to keep data packet in the queue. Otherwise, the state switches to transmit state to transmit data packet in the queue until it is empty. Then, the state is switched to sleep state.



At beginning, the state of USN is in sleep mode with no packet in memory buffer. When USN detects incoming packet, it is waked up and the system turned into idle state. USN receives the delivered packet when it's in idle state. To hold the packet in buffer memory, the power supply for USN cannot be stopped. When the number of packets in buffer memory is up to threshold N, the system changes to busy mode. The USN antenna module detects whether the radio channel is occupied and tries to access the channel. If it is failed, the USN receives the packet during waiting time. Otherwise, the system changes to transmit mode and the USN starts to transfer the packet in buffer memory.

3.3 System State Transformation

We adopted the birth-death graph technique to evaluate the probability for each state as shown in Figure 3. Each sensor node includes two queues (queue 1 and queue 2). The symbol (n_1, n_2) denotes the number of packets in the queue 1 and queue 2. For example, there is (0, 0) for the sleep state in the beginning, where both '0' represent that there isn't any data packet in the queue 1 and queue 2 at the start off phase. Similarly, the P_s , P_i , P_b , P_t and P_d represent the probability of sleep, idle, busy, transmit and drop states, respectively. We assume the average data input rate follows the Poisson distribution, where λ'_1 and λ'_2 are data input rate in respect with n1 and n2 packets for the idle state. Similarly, λ_1 and λ_2 are used to denote the data input rate for the other states. The μ_1 and μ_2 are used to indicate the average service rate for the n1 and n2 packets, respectively.

The system is in sleep mode (named as $P_s(0,0)$) in the beginning with empty buffer memory. When USN receives n1 or n₂ packet, the state enters into idle state named P_i . The amount of packet in buffer memory of queue 1 and queue 2 are less than N. If N is set to 4, queue 1 with three n₁ packets and queue 2 with two n₂ packets, it is named as $P_i(3,2)$. If queue1 receives one n₁ packet, the amount of n₁ will reach 4 and the system enters into busy state. The system tries to access the radio channel. If it is successful, the system enters into transmit mode. Otherwise, it receives packets until the number of packets in any of the buffer memory is reached to the buffer maxima size. After that, the income packet will be dropped because the buffer memory is full. The P_d indicates that the probability of dropping data if the queue is not available. The packet in queue will be transmitted with rate of μ_1 or μ_2 if the radio channel is available. The USN transfers all queue 1 and queue 2 packets following the priority in transmit mode.



Figure 3: System state transformation

3.4 Balance Formulation

To obtain the balance formula, we follow the method of induction. Based on the Figure 3, we derivate twenty-five general formulas by using graph with the case of N=4 and K=7, where N is the threshold value and K is the maxima size of buffer.

For the case 1 as Figure 4 (a) shows, the formula 1 shows the balance equation for the sleep state Ps(0,0), where the leave expectation value $P_s(0,0) \left(\lambda'_1 + \lambda'_2\right)$ is equal to the incoming expectation value from transmit state $P_t(1, 0)$ or $P_t(0, 1)$. The $P_t(1, 0)$ and $P_t(0, 1)$ will switch to $P_s(0, 0)$ if the data packet is transmitted out from buffer memory with rate μ_1 or μ_2 .

$$P_{s}(0,0)\left(\lambda'_{1}+\lambda'_{2}\right) = P_{t}(1,0)\,\mu_{1} + P_{t}(0,1)\,\mu_{2}\,\dots\dots\dots(1)$$

In Figure 4 (b), the balance equation of cases 2 can be expressed as formulas 2 and 3. The input expectation value and output expectation value are identical for $P_i(1,0)$ and $P_i(0,1)$. The balance equation in Figure 4 (c) can be expressed as:

 $P_i(3,0) \left(\lambda_1 + \lambda_2 \right) = P_i(3-1,0) \lambda_1 \dots (4)$ 2 \le 3 \le 4 - 1

,where the "3" and "3-1" can be replaced as n₁ and n₁-1, respectively for a general case as formula 4 shows. Similarly, the formula 5 can be obtained with the same method according to the Figure 4 (d). Again, the balance equation for the case 4 is: $P_i(2,2) \left(\lambda_1 + \lambda_2\right) = P_i(2,2-1) \lambda_2 + P_i(2-1,2) \lambda_1$, where n₁ and n₂ are identical to 2 in Figure 4 (e). The general form can be written as formula 6.

$$P_{i}(1,0)\left(\lambda_{1}+\lambda_{2}\right)=P_{s}(0,0)\lambda_{1}^{\prime}....(2)$$

$$P_{i}(0,1)(\lambda_{1} + \lambda_{2}) = P_{s}(0,0)\lambda_{2}' \qquad (3)$$

$$P_{i}(0, n_{2})(\lambda_{1} + \lambda_{2}) = P_{i}(0, n_{2} - 1) \lambda_{2}$$
(5)

$$2 \leq n_{2} \leq N - 1$$

$$P_{i}(n_{1}, n_{2})(\lambda_{1} + \lambda_{2}) = P_{i}(n_{1}, n_{2} - 1) \lambda_{2} + P_{i}(n_{1} - 1)$$

$$n_{2}(\lambda_{1} + \lambda_{2}) = P_{i}(n_{1}, n_{2} - 1) \lambda_{2} + P_{i}(n_{1} - 1)$$

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$$n_{3}(\lambda_{1} + \lambda_{2}) = P_{i}(n_{1}, n_{2} - 1) \lambda_{2} + P_{i}(n_{1} - 1)$$

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$$n_{3}(\lambda_{1} + \lambda_{2}) = P_{i}(n_{1} + \lambda_{2}) + P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{1} + \lambda_{2}) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{1} + 1) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{2} - 1) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{1} - 1) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{2} - 1) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{1} - 1) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{2} - 1) = P_{i}(n_{1} - 1)$$

$$n_{3}(\lambda_{2} - 1) = P_{i}(n_{1} - 1)$$

$$n_$$



Figure 4 (a), (b), (c) and (d): System state transformed from sleep mode to idle mode



Figure 4 (e) Case 4: System state transformed from idle mode to busy mode

Formulas 7 to 18 are balance equation for the busy state. Its range involves the transition from $P_b(N, 0)$ and $P_b(0, N)$ to $P_b(K, K)$. Based on the birth-death graph, we derivate the formulas 7 to 18 by using the same deductive method based on the Figure 4 (f) to (n). For example, in Figure 4 (l) of case 10, the balance equation is shown as: $P_b(7, 2) \begin{bmatrix} \lambda \\ \lambda \end{bmatrix}$

+
$$\mu_1(1-P_c)$$
] = $P_b(7,2-1)\lambda_1 + P_b(7-1,2)\lambda_1$
1 < 2 < 7 - 1.

In this case, the n_2 and K is equal to 2 and 7, respectively. The general form can be shown as formula 16.



Figure 4(f) Case 5 Figure 4 (g) Case 6 Figure 4 (h) Case 7

The balance equations for the transmit state can be listed as formulas 20 to 25. For example, the case 12 in Figure 4 (o), its balance equation is:

 $P_t(3,0) \mu_1 = P_b(3+1,0) \mu_1(1-P_c) + P_t(3+1,0) \mu_1$ and the n₂ should satisfy the first condition like $4-1 \le 3 \le 7-2$ & $0 \le 0 \le 4-1$ since it is in the light blue area, where n₁ and n₂ is equal to 3 and 0 respectively. The conditions for the purple and cyan areas are listed with respect to $1 \le n_1 \le N - 2$ & $N \le n_2 \le K$ and $N - 1 \le n_1 \le K - 2$ & $N \le n_2 \le K$. So, the n₁ and n₂ are located either in one of these conditions. Hence, the general form can be obtained as formula 20 shows.



Figure 4 (f)~4 (n): System state transformed from busy mode to transmit mode



Figure 4 (o) Case 12: System transmit state

$$\begin{split} & P_{b}(N,0) \left[\lambda_{1} + \lambda_{2} + \mu_{1} (1 - P_{c}) \right] = P_{i}(N - 1,0) \lambda_{1} \dots (7) \\ & P_{b} \left(N, n_{2} \right) \left[\lambda_{1} + \lambda_{2} + \mu_{1} (1 - P_{c}) \right] = P_{i} \left(N - 1, n_{2} \right) \lambda_{1} \\ & + P_{b} \left(N, n_{2} - 1 \right) \lambda_{2} \dots (8) \\ & 1 \leq n_{2} \leq N - 1 \end{split}$$
 $\begin{aligned} & P_{b}(0,N) \left[\lambda_{1} + \lambda_{2} + \mu_{2} (1 - P_{c}) \right] = P_{i}(0,N - 1) \lambda_{2} \dots (9) \\ & P_{b} \left(n_{1},N \right) \left[\lambda_{1} + \lambda_{2} + \mu_{1} (1 - P_{c}) \right] = P_{i} \left(n_{1},N - 1 \right) \lambda_{2} \end{split}$

$$\begin{aligned} &+P_{b}\left(n_{1}-1,N\right)\lambda_{1} \dots (10) \\ &1 \leq n_{1} \leq N-1 \\ \\ &P_{b}\left(n,0\right)\left[\lambda_{1}+\lambda_{2}+\mu_{1}\left(1-P_{c}\right)\right]=P_{b}\left(n_{1}-1,0\right) \dots (11) \\ &N+1 \leq n_{1} \leq K-1 \\ \\ &P_{b}\left(0,n_{2}\right)\left[\lambda_{1}+\lambda_{2}+\mu_{2}\left(1-P_{c}\right)\right]=P_{b}\left(0,n_{2}-1\right)\lambda_{2} \\ &\dots (12) \\ &N+1 \leq n_{2} \leq K-1 \\ \\ &P_{b}\left(n_{1},n_{2}\right)\left[\lambda_{1}+\lambda_{2}+\mu_{1}\left(1-P_{c}\right)\right]=P_{b}\left(n_{1}-1,n_{2}\right)\lambda_{1} \\ &+P_{b}\left(n_{1},n_{2}-1\right)\lambda_{2} \dots (13) \\ &N+1 \leq n_{1} \leq K-1 &\& 1 \leq n_{2} \leq N \\ &1 \leq n_{1} \leq N &\& N+1 \leq n_{2} \leq K-1 \\ &N+1 \leq n_{1} \leq K-1 &\& N+1 \leq n_{2} \leq K-1 \\ &n_{1} = N &\& n_{2} = N \\ \\ &P_{b}(K,0)\left[\lambda_{2}+\mu_{1}\left(1-P_{c}\right)\right]=P_{b}(K-1,0)\lambda_{1} \dots (14) \\ &P_{b}(0,K)\left[\lambda_{2}+\mu_{1}\left(1-P_{c}\right)\right]=P_{b}(K,n_{2}-1)\lambda_{2} + \\ &P_{b}(K-1,n_{2})\lambda_{1} \dots (16) \\ &1 \leq n_{2} \leq K-1 \\ \\ &P_{b}\left(n_{1},K\right)\left[\lambda_{1}+\mu_{1}\left(1-P_{c}\right)\right]=P_{b}\left(n_{1}-1,K\right)\lambda_{1} + \\ &P_{b}\left(n_{1},K-1\right)\lambda_{2} \dots (17) \\ &1 \leq n_{2} \leq K-1 \\ \\ &P_{b}(K,K)\left[\mu_{1}\left(1-P_{c}\right)\right]=P_{b}(K-1,K)\lambda_{1} + P_{b}(K,K-1) \\ &\lambda_{2} \dots (17) \\ &1 \leq n_{2} \leq K -1 \\ \\ &P_{b}(K,K)\left[\mu_{1}\left(1-P_{c}\right)\right]=P_{b}(K-1,K)\lambda_{1} + P_{b}(K,K-1) \\ &\lambda_{2} \dots (17) \\ &1 \leq n_{1} \leq K-2 \\ \\ &P_{t}\left(n_{1},n_{2}\right)\mu_{1} =P_{b}\left(n_{1}+1,n_{2}\right)\mu_{1}\left(1-P_{c}\right) + P_{t}\left(n_{1}+1,n_{2},\mu_{1},\mu_{1}-P_{c}\right) \\ &N-1 \leq n_{1} \leq K-2 \\ \\ &N-1 \leq n_{1} \leq K-2 \\ \\ &N-1 \leq n_{1} \leq K-2 \\ \\ &N \leq n_{2} \leq K \\ \\ &P_{t}(0,K)\mu_{2} = P_{t}\left(1,N_{1}\right)\mu_{1} + P_{t}\left(0,n_{2}+1\right)\mu_{2} + \\ \\ &P_{b}(0,N-1)\mu_{2} = P_{t}(1,N-1)\mu_{1} + P_{t}(0,N)\mu_{2} + \\ \\ &P_{t}(0,N-1)\mu_{2}\left(1-P_{c}\right) \dots (23) \\ \end{aligned}$$

$$P_{t}(0, n_{2}) \mu_{2} = P_{t}(1, n_{2}) \mu_{1} + P_{t}(0, n_{2} + 1) \mu_{2} \dots (24)$$

$$1 \le n_{2} \le N - 2$$

$$P_{t}(n_{1}, n_{2}) \mu_{1} = P_{t}(n_{1} + 1, n_{2}) \mu_{1} \dots (25)$$

$$1 \le n_{1} \le N - 2 \& 0 \le n_{2} \le N - 1$$

3.5 Ps Probability

To evaluate the correctness of formulas mentioned in previous section, we calculate the $P_s(0,0)$ firstly. $P_s(0,0)$ represents the probability where there is no n_1 or n_2 packet transmitted into system during a period of T. The Poisson formula is as:

$$Poisson(x) = \frac{e^{-\lambda t} (\lambda t)^x}{x!}$$

This formula represents the probability of entering x packets during $0 \sim t$. There is no packet cached into the queue of sensor node during the sleep state, so the number of packets x can be set to 0. The t is set to T because we consider the average value during one cycle period. In addition, the packet transmit rate for n_1 and n_2 are assumed as λ_1 and λ_2 , respectively. Thus, the probability of n_1 packet not cached is:

$$P_s = \text{Poisson}(0) = e^{-\lambda_1 T}$$

Similarly, the probability of n₂ not cached is:

$$P_s = \text{Poisson}(0) = e^{-\lambda_2 T}$$

The probability of no packet n_1 and n_2 :

 $\left(e^{-\lambda_1 T}\right)\left(e^{-\lambda_2 T}\right)....(26)$

The probability of packet n_1 cached but no n_2 packet : $(1 - e^{-\lambda_1 T})(e^{-\lambda_2 T})$(27)

The probability of packet
$$n_2$$
 cached but no n_1 packet :
 $(1 - e^{-\lambda_2 T})(e^{-\lambda_1 T})$(28)

The probability of packets $n_1 \mbox{ and } n_2$ cached simultaneously :

$$\left(1-e^{-\lambda_1 T}\right)\left(1-e^{-\lambda_2 T}\right).$$
(29)

Because the summation of formulas (26), (27), (28) and (29) is 1 and the case of formula (29) will not occur, the probability can be written as:

 $1 - (1 - e^{-\lambda_1 T})(1 - e^{-\lambda_2 T})$(30) Thus, the probability of no packets n_1 and n_2 cached can be derived as:

$$P_{S}(0,0) = \frac{e^{-\lambda_{1}T} \times e^{-\lambda_{2}T}}{1 - (1 - e^{-\lambda_{1}T})(1 - e^{-\lambda_{2}T})}.....(31)$$

3.6 System Power Consumption Formula

The system power consumption during a life cycle can be obtained as:

$$\begin{split} F(N) &= C_{hold}L_N + \frac{C_{setup}}{T} + C_{idle}P_i + C_{busy}P_b + C_{sleep}P_s + \\ C_{transmit}P_t & \dots & (32) \\ \text{, where the related parameters are explained as Table 1:} \end{split}$$

Table 1 Explanation of Parameter

Parameter	Explanation
C _{hold}	The power of holding packet in system
	memory
C _{setup}	The power needed for recovering from sleep
	to idle state
C _{sleep}	The power consumption when system in
	sleep state
C _{idle}	The power consumption when system in idle
	state
C _{busy}	The power consumption when system in busy
	state
C _{transmit}	The power consumption when system in
	transmit state
L _N	The number of packets in queue
Т	A period length
Ps	The probability of sleep state
Pi	The probability of idle state
Pb	The probability of probability state
Pt	The probability of transmit state

, where $L_N = L_{sleep} + L_{idle} + L_{busy} + L_{transmit}$(33) Its related parameters are explained as shown in Table 2.

Table 2 Parameters of L_N

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Parameter	Explanation
L _{sleep}	The number of packets in sleep state, $L_{sleep} =$
	0 since there is no packet in the queue at the
	sleep state
L _{idle}	The number of packets in idle state
L _{busy}	The number of packets in busy state
L _{transmit}	The number of packets in transmit state

3.7 Packet Delay Formula

The time period between the time of packet entered into the queue of sensor node and the time of packet left from the sensor node is defined as packet delay time. In this paper, we discuss the n_1 and n_2 packets and its packet delay formula. To derivate the delay formula, there are several definitions should be provided as:

 P_i : the probability of idle state.

 $P_i[n_1]$: the probability of idle state having queue 1 packet but no queue 2 packet

 $P_i[n_2]$: the probability of idle state having queue 2 packet but no queue 1 packet

 $P_i[n_1 + n_2]$: the probability of idle state having queue 1 and queue 2 packets

 P_b : the probability of busy state

 $P_b[n_1]$: the probability of busy state having queue 1 packet but no queue 2 packet

 $P_b[n_2]$: the probability of busy state having queue 2 packet but no queue 1 packet

 $P_b[n_1 + n_2]$: the probability of busy state having queue 1 and queue 2 packets

 P_t : the probability of transmit state

 $P_t[n_1]$: the probability of transmit state having queue 1 packet but no queue 2 packet

 $P_t[n_2]$: the probability of transmit state having queue 2 packet but no queue 1 packet

 $P_t[n_1 + n_2]$: the probability of transmit state having queue 1 and queue 2 packets

The delay time of n_1 packet :

Busy : P_b represents the probability in busy state. The probability of queue 1 with no packet and queue 2 having packet is denoted as $P_b[n_2]$. The delay time expectation for n1 packet in busy state is :

 $(P_b - P_b[n_2]) \times T.$ (35)

Transmit: P_t represents the probability in transmit state. The probability for queue 1 with no packet and queue 2 with packet is $P_t[n_2]$. The delay time expectation for n_1 packet in the transmit state until it has been transmitted is :

By summing (34), (35), and (36), the n_1 packet delay time can be obtained as :

Similarly, the n_2 packet delay time can be derived as follows :

Idle: P_i represents the probability in idle state. The probability of queue 1 with packet and queue 2 with no packet is $P_i[n_1]$. The delay time expectation for n_2 packet in the idle state is:

 $(P_i - P_i[n_1]) \times T \dots (38)$

Busy: P_b represents the probability of packet in busy state. $P_b[n_1]$ is the probability of queue 1 with packet and queue 2 with no packet. The delay expectation for packet n_2 in busy state is:

 $(P_b - P_b[n_1]) \times T$(39)

Transmit: P_t represents the probability of packet in transmit state. $P_t[n_1]$ is the probability of queue 1 with packet and queue 2 with no packet. Similarly, $P_t[n_2]$ is the probability of queue 2 with packet and queue 1 with no packet. $P_t[n_1 + n_2]$ denotes that both queue 1 and queue 2 have data packet. The packet in queue 2 has to wait until the packet in queue 1 has been transmitted. The delay time expectation of n_2 packet is obtained as:

 $(P_t[n_1 + n_2]) \times T + \frac{P_t[n_2]}{2} \times T$ (40) By combining (38) (39) and (40), the n₂ packet delay time is:

$$\left((P_i - P_i[n_1]) + (P_b - P_b[n_1]) + (P_t[n_1 + n_2]) + \frac{P_t[n_2]}{2} \right) T \dots$$
(41)

4. Experimental Results

Formula 32 computes the energy consumption in one cycle. Five parameters: data input rate (λ), service rate (μ), collision rate (P_c), threshold (N) and queue size (K), are necessary in this formula to obtain the energy consumption. The value of parameters is changed to evaluate the relation between these parameters and probability for each state. The experiment is carried out with MatLab(version 7.11.0.584) on a IBM PC.

4.1 The variation of Input Data

To evaluate the influences of data arrival rate, the arrival rate (λ) is changed from 0.3 to 3.0 with step 0.3 in corresponding to service rate (μ)=0.3, collision probability (P_c)=0.1, threshold (N)=4 and queue size=7.

Figure 5 demonstrated that the system probability at sleep mode becomes small when the data arrival rate is increased. The USN has higher opportunity to receive data packet as well as to be woken up. The probability in idle state also becomes smaller because of receiving data quickly make the number of data in queue to be threshold N. The state is turned into busy mode. There are no close relation between arrival rate and busy state probability is increased proportional to the data arrival rate (λ) since the service rate (μ) is less than arrival rate to result in staying at transmit state longer.



Figure 5: Data input rate(λ) and the variation of probability in different state

4.2 The Variation of System Service Rate

To evaluate the influence of changing service rate (μ) form 0.3 to 3, we assign the arrival rate (λ)=0.3,collision probability (P_c)=0.1, threshold (N)=4 and queue size(K)=7. The experimental result in Figure 6, it displays that the transmit probability is decreased if the service rate (μ) is increased. The probability toward the sleep state is increased as well as the idle state because of fixed arrival rate. The probability of busy state is decreased due to increasing service rate.

4.3 The Variation of Packet Collision Probability

In this experiment as Figure 7 shows, we change the collision probability form 0.1 to 0.9 by step 0.1 when assuming service rate (μ)=0.3, arrival rate (λ)=0.3, threshold (N)=4 and queue size (K)=7. The changing

collision probability has big influence on the probability of busy state. The bigger busy state probability indicates that stay at the busy state longer. The probability for the rest state becomes small due to busy state probability increased.



Figure 6: System service rate (μ) and the variation of probability in different state



Figure 7: The probability of packet collision (P_c) and the variation of probability in different state

4.4 The Variation of Queue Threshold

In Figure 8, we change the value of threshold from 3 to k-2 when assuming service rate (μ)=0.3, arrival rate (λ)=0.3 and queue size (K)=12. The results show when the threshold is increased, the USN received more packets for turning its state from busy to idle. This increases the value of P_i. The higher value of the threshold is, the lower differences between N and K. This results in the probability of busy state reduced. Similarly, the probability of transmission state is also reduced because of more packets in queue for transmission.



Figure 8: Queue threshold (N) and the variation of probability in each state

4.5 The Threshold N of Lowest Power Consumption

The threshold (N) of lowest power consumption is computed in this experiment,. The parameters for this experiment is: (N)=3~K-2, (μ)=0.3, (λ)=0.3, (P_c)=0.1 and (K)=12. Because the system power consumption should be calculated, the parameters are set as: C_{hold}=5, C_{setup}=300, C_{idle}=50, C_{busy}=500, C_{sleep}=1 and C_{transmit}=500.

Figure 9 shows that system power is in the lowest state when threshold is set to 6. This is useful for the parameter of setting threshold (N) for lowest power consumption to extend the life cycle of USN.



Figure 9: The threshold (N) of the lowest power consumption

4.6 Packet Delay Time

In this experiment, the packet delay time is computed with the parameters: (N)=3~K-2, (μ)=0.3, (λ)=0.3, (P_c)=0.1, (K)=12. Figure 9 is the probability of two packets with different priorities stayed in sensor node. The packet delay time is calculated by multiplying T (working period). In Figure 10, n₁ is the probability of packet with higher priority whose delay time is lower than n₂.



Figure 10: The packet delay time with a single sensor node

Figure 11 is the delay time when a packet transferred through three and ten sensor nodes. The higher value of N is, the longer time of packet is delayed. The delay time gap would be higher if the transfer frequency is increased.

5. Conclusions

In this research, we proposed a method for increasing the available time of system with lower cost by extending the usage of battery power. The sleep mode and limited queue of system is adopted in this research. By quantizing the variables of system power consumption, the best value of queue threshold can be obtained. This is useful for extending the power of USN. Besides, the priority is applied to the ubiquitous computing of packet. In this way, packet with higher priority can be transferred faster. This can be applied to the system with real time reaction.



Figure 11: The delay time with numerous sensor nodes

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