

# An ABC Supported QoS Multicast Routing Scheme Based on Beehive Algorithm

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## ABSTRACT

In this paper, a QoS multicast routing scheme with ABC (Always Best Connected) supported is proposed based on the beehive algorithm. To deal with the inaccurate network status and the imprecise user QoS requirement, the proposed scheme uses the range to describe them, introduces the edge bandwidth pricing, the edge evaluation and the tree evaluation, and tries to find a QoS multicast tree with the Pareto optimum under the Nash equilibrium on both the network provider utility and the user utility achieved or approached. Simulation results have shown that it is both feasible and effective.

## Categories and Subject Descriptors

C.2.1 [COMPUTER-COMMUNICATION NETWORKS]: Network Architecture and Design –*Network communications*

## General Terms

Algorithms, Performance, Design

## Keywords

QoS (Quality of Service) Multicast Routing, ABC (Always Best Connected), Beehive Algorithm, Nash Equilibrium, Pareto Optimum

## 1. INTRODUCTION

NGI (Next Generation Internet) is now becoming an integrated network converged seamlessly by heterogeneous multi-segment multi-provider sub-networks, such as terrestrial-based, space-based, fixed and mobile ones. Its backbone and access links become diversified. Several different kinds of links may coexist on each hop for a user to choose when routing. It is possible for a user to be ABC (Always Best Connected) [1] to NGI in the course of communication and thus the so-called global QoS (Quality of Service) roaming should be supported seamlessly.

ABC means that a user can connect with NGI anytime, anywhere in the currently best way and switch to the better way adaptively and transparently whenever it comes forth. However, 'best' is a fuzzy concept, depending on many factors, such as user QoS

requirement, cost a user willing to pay and user preference. In addition, with the gradual commercialization of the network operation, both the network provider and the user profit should be considered with their utility win-win supported. At the same time, NGI's heterogeneity and dynamics, terminal and even network mobility, unavoidable message transfer delay and its uncertainty make it hard to describe the network status exactly and completely [2]. The user QoS requirement is affected largely by a lot of subjective factors and often can not be expressed accurately, thus the flexible QoS description is needed. All these make it hard to provide QoS multicast routing with ABC supported in NGI.

QoS multicast routing has been proven to be NP-complete [3]. Many heuristic and intelligent optimization algorithms have been used to solve it. In [4], a QoS-aware algorithm is proposed to find the multicast routing tree by constructing the constraint vector with the parallel multiple paths searching. In [5], a heuristic QoS multicast routing algorithm is presented. It adopts distributed computing and routing label to reduce its time complexity. However, the inaccurate network status and the utility optimization of both the user and the network provider are not taken into account in [4, 5]. In [6], a multi-constrained QoS multicast routing algorithm under the inaccurate information is introduced. It uses the improved Bellman-Ford algorithm for routing. In [7], based on the probability theory, GA (Genetic algorithm) is used to find the optimal multicast routing tree under the inaccurate information. In [8], the fuzzy set is used to describe the inaccurate link state, and the multicast routing tree is built based on GA with the fuzzy measures introduced. Nevertheless, the proposed algorithms in [6, 7, 8] only consider meeting the user QoS requirement and do not consider achieving utility win-win between the user and the network provider. In [9], the SPEA (Strength Pareto Evolutionary Algorithm) is proposed to build a tree with the Pareto optimum. It considers the user utility, but does not consider the network provider utility. In [10], the utility function and the pricing scheme are introduced to make the multicast resource allocation fairly. However, its focus is on the network congestion control and not on the multicast routing. It also does not consider the inaccurate network status. In [11], a fair QoS multicast routing scheme is proposed with a Kelly/PSP model based pricing scheme introduced. Its focus is to solve the multicast fairness issue, not dealing with utility win-win between the user and the network provider and not considering the inaccurate network status.

By far, how to provide a QoS multicast routing scheme to support utility win-win between the user and the network provider under the imprecise network status and the inaccurate user QoS requirement from ABC viewpoint has not got much attention. In this paper, a QoS multicast routing scheme with ABC supported

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is proposed. In order to deal with the imprecise network status information and the flexible user QoS requirement, the range is used to describe them and the edge bandwidth pricing, the edge evaluation and the multicast tree evaluation are introduced. Based on the beehive algorithm [12], the proposed scheme tries to find a QoS multicast tree with Pareto optimum under Nash equilibrium on both the network provider utility and the user utility achieved or approached.

## 2. Model Description

### 2.1 Network Model and Routing Request

A network can be modeled as a graph  $G(V, E)$ ,  $V$  is the node set and  $E$  is the edge set.  $\forall v_i, v_j \in V$ , there maybe exist several edges to represent different kinds of links between them,  $i, j = 1, \dots, |V|$ . Just for simplicity, the node parameters are merged into the edge ones.  $\forall e_l \in E$ , consider the following parameters: network provider number  $z$ , total bandwidth  $tbw_l$ , available bandwidth  $bw_l$ , delay  $dl_l$ , delay jitter  $jt_l$ , error rate  $ls_l$ , bandwidth unit cost  $ct_l$  and bandwidth price  $p_l$ .  $z \in NPS$  and  $NPS$  is the set of all network provider numbers. A QoS multicast routing request is denoted as  $\langle v_s, D, R_{Bw}, R_{Dl}, R_{Jt}, R_{Ls}, PY, BD \rangle$ .  $v_s \in V$  is its source node;  $D = \{v_{d_1}, \dots, v_{d_{|D|}}\} \in V$  is its destination node set;  $R_{Bw} = (\Delta_{Bw_1}, \dots, \Delta_{Bw_{|D|}})$ ,  $R_{Dl} = (\Delta_{Dl_1}, \dots, \Delta_{Dl_{|D|}})$ ,  $R_{Jt} = (\Delta_{Jt_1}, \dots, \Delta_{Jt_{|D|}})$  and  $R_{Ls} = (\Delta_{Ls_1}, \dots, \Delta_{Ls_{|D|}})$  are its bandwidth, delay, delay jitter and error rate requirement vectors, with  $\Delta_{Bw_i} = [BW_i^L, BW_i^H]$ ,  $\Delta_{Dl_i} = [DL_i^L, DL_i^H]$ ,  $\Delta_{Jt_i} = [JT_i^L, JT_i^H]$  and  $\Delta_{Ls_i} = [LS_i^L, LS_i^H]$  representing bandwidth, delay, delay jitter and error rate requirement of the multicast user attached to  $v_{d_i}$  (below just use the term 'the  $i_{th}$  user' simply). The actually received QoS of one user from one edge is classified into four levels:  $QL = \{\text{Excellent, Good, Fair, Poor}\}$ .  $PY = (py_1, \dots, py_{|D|})$  and  $BD = (bd_1, \dots, bd_{|D|})$  are the expenditure and bid vectors each user willing to pay and offer, with  $py_i \in \{py_{ie}, py_{ig}, py_{if}, py_{ip}\}$  and  $bd_i \in \{bd_{ie}, bd_{ig}, bd_{if}, bd_{ip}\}$  corresponding to the specific expenditure and bid the  $i_{th}$  user willing to pay and offer when the  $i_{th}$  user actually received QoS level from  $e_l$  is a specific value  $Ql_{il}$  from  $QL$ . Here, it is assumed that a QoS multicast routing request is heterogeneous, that is, each user has different requirement on QoS, expenditure and bid. If it is homogeneous, that is, each user has the same requirement,  $R_{Bw}, R_{Dl}, R_{Jt}, R_{Ls}$ ,  $PY$  and  $BD$  all only have one element.

In this paper, the objective of the proposed scheme is to find a QoS multicast tree  $T_{sD}$  with  $v_s$  as its root and  $v_{d_i} \in D$  as its leaf, making the Pareto optimum under the Nash equilibrium between the user utility and the network provider utility along  $T_{sD}$  as well as the minimum cost of  $T_{sD}$  achieved or approached.

### 2.2 Bandwidth Pricing

To promote a user to consume bandwidth rationally, the edge bandwidth price can be divided into three regions, i.e., low, sound and high [13]. Assume  $\eta_l$  represents the loaded level of  $e_l$  and is calculated as follows:

$$\eta_l = 1 - \frac{bw_l}{tbw_l} \quad (1)$$

If  $\eta_l < \eta_l^0$ ,  $e_l$  is considered to be low-loaded, its bandwidth price is at the low region and can be adjusted according to the formula (2); if  $\eta_l > \eta_l^1$ ,  $e_l$  is considered to be high-loaded, its bandwidth price is at the high region and determined by bidding; otherwise,  $e_l$  is considered to be moderate-loaded, its bandwidth price is at the sound region and can be adjusted according to the formula (3).

$$p_l = \begin{cases} p_l^{\min} & \eta_l < \eta_l^{\min} \\ \frac{A}{1 + \alpha \times \eta_l^{-\beta}} & \eta_l^{\min} \leq \eta_l \leq \eta_l^0 \end{cases} \quad (2)$$

$$p_l = \begin{cases} p_l^{\max} & \eta_l^{\max} < \eta_l < \eta_l^1 \\ B \times (2 - e^{-\delta \times (\eta_l - \eta_l^0)^2}) & \eta_l^0 \leq \eta_l \leq \eta_l^{\max} \end{cases} \quad (3)$$

$\eta_l^0$  and  $\eta_l^1$  are preset values,  $0 < \eta_l^0 < \eta_l^1 < 1$ .  $p_l^{\min}$  and  $p_l^{\max}$  are the lower bound of the low region and the upper bound of the sound region of  $e_l$ ,  $\eta_l^{\min}$  and  $\eta_l^{\max}$  are their edge loaded level.

Use  $p_l^0$  to represent the bandwidth baseline price of  $e_l$ , its edge loaded level is  $\eta_l^0$ ,  $p_l^{\min} \leq p_l^0 \leq p_l^{\max}$ . For  $\eta_l^{\min} \leq \eta_l \leq \eta_l^0$ ,  $p_l$  is semi-rising Cauchy distribution alike with  $\beta = 2$  usually,  $p_l = p_l^0$  when  $\eta_l = \eta_l^0$  and  $p_l = p_l^{\min}$  when  $\eta_l = \eta_l^{\min}$  [14], thus  $A$  and  $\alpha$  can be calculated by the formula (4) and (5).

$$A = p_l^0 \times \left(1 + \frac{p_l^0 - p_l^{\min}}{p_l^{\min} \times (\eta_l^{\min})^{-2} - p_l^0 \times (\eta_l^0)^{-2}} \times (\eta_l^0)^{-2}\right) \quad (4)$$

$$\alpha = \frac{p_l^0 - p_l^{\min}}{p_l^{\min} \times (\eta_l^{\min})^{-2} - p_l^0 \times (\eta_l^0)^{-2}} \quad (5)$$

For  $\eta_l^0 \leq \eta_l \leq \eta_l^{\max}$ ,  $p_l$  is semi-rising normal distribution alike,  $p_l = p_l^0$  when  $\eta_l = \eta_l^0$  and  $p_l = p_l^{\max}$  when  $\eta_l = \eta_l^{\max}$  [14], thus  $B$  and  $\delta$  can be calculated by the formula (6) and (7).

$$B = p_l^0 \quad (6)$$

$$\delta = -\frac{\ln(2 - \frac{p_l^{\max}}{p_l^0})}{(\eta_l^{\max} - \eta_l^0)^2} \quad (7)$$

## 2.3 Adaptability Membership Degree

It is introduced to describe the adaptability of the edge status to the user QoS requirement. The bandwidth, delay, delay jitter and error rate adaptability membership degree function of  $e_l$  to the  $i_{th}$  user requirement are defined in the following formula (8) to (11).

$$g_{il}^1 = \begin{cases} 2 \times \left( \frac{bw_l - BW_i^L}{BW_i^H - BW_i^L} \right)^2 & BW_i^L < bw_l \leq \frac{(BW_i^H + BW_i^L)}{2} \\ 1 - 2 \times \left( \frac{BW_i^H - bw_l}{BW_i^H - BW_i^L} \right)^2 & \frac{(BW_i^H + BW_i^L)}{2} < bw_l \leq BW_i^H \\ 1 & bw_l > BW_i^H \end{cases} \quad (8)$$

$$g_{il}^2 = \begin{cases} 1 & dl_l \leq DL_i^L \\ \left( \frac{DL_i^H - dl_l}{DL_i^H - DL_i^L} \right)^k & DL_i^L < dl_l \leq DL_i^H \\ 0 & dl_l > DL_i^H \end{cases} \quad (9)$$

$$g_{il}^3 = \begin{cases} 1 & jt_l \leq JT_i^L \\ \left( \frac{JT_i^H - jt_l}{JT_i^H - JT_i^L} \right)^k & JT_i^L < jt_l \leq JT_i^H \\ 0 & jt_l > JT_i^H \end{cases} \quad (10)$$

$$g_{il}^4 = \begin{cases} 1 & ls_l \leq LS_i^L \\ \left( \frac{LS_i^H - ls_l}{LS_i^H - LS_i^L} \right)^k & LS_i^L < ls_l \leq LS_i^H \\ 0 & ls_l > LS_i^H \end{cases} \quad (11)$$

The formula (8) is  $S$  distribution alike and the formula (9), (10) and (11) are  $k$ -parabolic distribution alike, all having smooth transition feature [14].

## 2.4 Utility

### 2.4.1 User Utility

According to the formula (8) to (11), get the evaluation matrix  $G_{il} = [g_{il}^1 \ g_{il}^2 \ g_{il}^3 \ g_{il}^4]^T$  of the  $i_{th}$  user on  $e_l$ . The weight matrix  $\Lambda = [\lambda_1 \ \lambda_2 \ \lambda_3 \ \lambda_4]$  is given by the application nature,  $\lambda_1, \lambda_2, \lambda_3$  and  $\lambda_4$  are the relative significance weights of bandwidth, delay, delay jitter and error rate on the application QoS respectively,  $0 \leq \lambda_1, \lambda_2, \lambda_3, \lambda_4 \leq 1$ ,  $\lambda_1 + \lambda_2 + \lambda_3 + \lambda_4 = 1$ . The satisfaction degree  $St_{il}$  of the  $i_{th}$  user to the status of  $e_l$  is as follows:

$$St_{il} = \Lambda \circ G_{il} \quad (12)$$

The mapping between  $St_{il}$  and  $Ql_{il}$  is defined as follows:

$$Ql_{il} = \begin{cases} \text{Excellent} & St_{il} \geq \alpha_1 \\ \text{Good} & \alpha_2 \leq St_{il} < \alpha_1 \\ \text{Fair} & \alpha_3 \leq St_{il} < \alpha_2 \\ \text{Poor} & St_{il} < \alpha_3 \end{cases} \quad (13)$$

$\alpha_1, \alpha_2$  and  $\alpha_3$  are preset values. According to  $Ql_{il}$ ,  $py_i$  can be determined from  $\{py_{ie}, py_{ig}, py_{if}, py_{ip}\}$ .

The satisfaction degree  $SC_{il}$  of the  $i_{th}$  user to the expenditure he paid for using  $e_l$  is defined as follows:

$$SC_{il} = \begin{cases} 1 & p_l \times abw_l \leq \frac{1}{\chi} py_i \\ \left( \frac{py_i - p_l \times abw_l}{py_i - \frac{1}{\chi} py_i} \right)^k & \frac{1}{\chi} py_i < p_l \times abw_l \leq py_i \\ 0 & p_l \times abw_l > py_i \end{cases} \quad (14)$$

$abw_l$  is the actually allocated bandwidth for the  $i_{th}$  user on  $e_l$ ,  $BW_i^L \leq abw_l \leq BW_i^H$ ;  $\chi$  is a tuning factor,  $\chi > 1$ ,  $k$  is preset value. The  $i_{th}$  user utility on  $e_l$  is as follows:

$$uu_{il} = \varpi_1 \times St_{il} + \varpi_2 \times SC_{il} \quad (15)$$

$\varpi_1$  and  $\varpi_2$  are preference weights on  $St_{il}$  and  $SC_{il}$ ,  $0 \leq \varpi_1, \varpi_2 \leq 1$ ,  $\varpi_1 + \varpi_2 = 1$ .

### 2.4.2 Network Provider Utility

Assume that there are  $k$  edges owned by the different network providers between two nodes and consider the following attributes for each edge: available bandwidth, delay, delay jitter, error rate, loaded level, bandwidth price and being\_selected\_probability, constituting a  $k \times 7$  evaluation matrix  $F_{k \times 7}$ . Its element  $f_{zy}$  represents the  $y_{th}$  attribute of the edge provided by the  $z_{th}$  network provider,  $1 \leq z \leq k, 1 \leq y \leq 7$ . Do normalization to 'the larger the better' and 'the smaller the better' attributes according to the formula (16) and (17).

$$f'_{zy} = \frac{f_{zy}}{f_{\max,y} + f_{\min,y}} \quad (16)$$

$$f'_{zy} = \frac{f_{\max,y} + f_{\min,y} - f_{zy}}{f_{\max,y} + f_{\min,y}} \quad (17)$$

$$f_{\min,y} = \min_z \{f_{zy}\} \quad (18)$$

$$f_{\max,y} = \max_z \{f_{zy}\} \quad (19)$$

$f_{\min,y}$  and  $f_{\max,y}$  are the minimum and maximum of the  $y_{th}$  attribute value.

The network provider utility is calculated as follows:

Step1: Construct the evaluation matrix  $F_{k \times 7}$ .

Step2: Modify  $F_{k \times 7}$  as follows: normalize the delay, delay jitter, error rate and loaded level according to the formula (17) and the available bandwidth, bandwidth price and being\_selected\_probability according to the formula (16).

Step3: Calculate the standard deviation  $s_y$  for each attribute according to the formula (20), compute the weight for each attribute according to the formula (22).

$$s_y = \left( \frac{1}{k} \times \sum_{z=1}^k (f'_{zy} - \overline{f_y})^2 \right)^{\frac{1}{2}} \quad (20)$$

$$\overline{f_y} = \frac{1}{k} \times \sum_{z=1}^k f'_{zy} \quad (21)$$

$$w_y = \frac{s_y}{\sum_{\kappa=1}^7 s_{\kappa}} \quad (22)$$

Step4: Calculate the  $z_{th}$  network provider utility  $nu_{z_l}$  on  $e_l$  according to the formula (23).

$$nu_{z_l} = \sum_{y=1}^7 w_y \times f'_{zy} \quad (23)$$

## 2.5 Gaming Analysis

The network provider and the user play game on the edge. Each network provider has two gaming strategies: whether he is willing to provide the edge to the user or not. The user also has two gaming strategies: whether he is willing to accept the provided edge or not. The gaming matrixes of the  $i_{th}$  user and the  $z_{th}$  network provider on  $e_l$  are as follows:

$$UU_{il} = \begin{bmatrix} \ln \frac{uu_{il}}{uu_{il_0}} & \gamma \times \ln \frac{uu_{il}}{uu_{il_0}} \\ -\mu \times \ln \frac{uu_{il}}{uu_{il_0}} & 0 \end{bmatrix} \quad (24)$$

$$NU_{z_l} = \begin{bmatrix} \ln \frac{nu_{z_l}}{nu_{z_l_0}} & -\mu \times \ln \frac{nu_{z_l}}{nu_{z_l_0}} \\ \gamma \times \ln \frac{nu_{z_l}}{nu_{z_l_0}} & 0 \end{bmatrix} \quad (25)$$

The rows in  $UU_{il}$  and  $NU_{z_l}$  correspond to the  $i_{th}$  user gaming strategies: accept or not, the columns correspond to the  $z_{th}$  network provider gaming strategies: provide or not.  $uu_{il_0}$  and  $nu_{z_l_0}$  represent the lowest acceptable utilities of the  $i_{th}$  user and the  $z_{th}$  network provider on  $e_l$ . If the  $z_{th}$  network provider is willing to provide  $e_l$  but the  $i_{th}$  user rejects  $e_l$  or the  $i_{th}$  user is willing to accept  $e_l$  but the  $z_{th}$  network provider does not provide  $e_l$ , the  $i_{th}$  user or the  $z_{th}$  network provider should be punished. Here,  $\mu$  is a penalty factor bigger than 1. If the  $z_{th}$  network provider does not provide  $e_l$  but the  $i_{th}$  user is willing to accept  $e_l$  or the  $i_{th}$  user rejects  $e_l$  but the  $z_{th}$  network provider is willing to provide  $e_l$ , the  $z_{th}$  network provider utility or the  $i_{th}$  user utility would be suffered,  $\gamma$  is a loss factor smaller than 1. If the  $z_{th}$  network provider does not provide  $e_l$  at the same time the  $i_{th}$  user rejects  $e_l$ , both utilities are 0. If the strategy

pair  $\langle p^*, q^* \rangle$  satisfies the formula (26), it is a specific solution under Nash equilibrium [15]:

$$\begin{cases} uu_{p^*q^*} \geq uu_{pq^*} \\ nu_{p^*q^*} \geq nu_{p^*q} \end{cases} \quad (26)$$

If  $\langle p^*, q^* \rangle$  is  $\langle \text{accept}, \text{provide} \rangle$ ,  $e_l$  will be selected, otherwise aborted,  $p, q, p^*, q^* = 1, 2$ .

## 2.6 Being\_selected\_probability

Its initial value of  $e_l$  is calculated as follows:

$$pr_i^0 = \frac{1}{SE_l} \quad (27)$$

$SE_l$  is the number of those edges sharing the same endpoints with  $e_l$ . All edges sharing the same endpoints have the same being\_selected\_probability initially. When routing, it is updated as follows:

$$pr_i^j = \frac{SS_j^2}{SS_j^2 + \theta_j^2} \quad (28)$$

$$SS_j = \begin{cases} \omega_1 SS_0 + \omega_2 \times \frac{\tau}{HP_j(sn(e_l), v_t)} & \text{the } j_{th} \text{ bee passing } e_l \\ SS_0 & \text{otherwise} \end{cases} \quad (29)$$

$$\theta_j = \begin{cases} \omega_3 \theta_0 + \omega_4 \times \lambda \times HP_j(sn(e_l), v_t) & \text{the } j_{th} \text{ bee passing } e_l \\ \theta_0 + \sigma \times HP_j(sn(e_l), v_t) & \text{otherwise} \end{cases} \quad (30)$$

$SS_j$  is stimulation signal value produced by the  $j_{th}$  bee,  $SS_0$  is baseline value,  $sn(e_l)$  is starting endpoint of  $e_l$ ,  $v_t$  is another endpoint along the path having traversed by the  $j_{th}$  bee,  $HP_j(sn(e_l), v_t)$  is hop count between  $sn(e_l)$  and  $v_t$  along the path from  $v_s$  to  $v_t$ ,  $\theta_j$  is its own reaction valve value to  $v_{d_i}$  of the  $(j+1)_{th}$  bee,  $\theta_0$  is its baseline value,  $\omega_1, \omega_2, \omega_3$  and  $\omega_4$  are preference weights,  $\tau, \lambda$  and  $\sigma$  are constants,  $\tau > 1, 0 < \lambda, \sigma < 1, 0 \leq \omega_1, \omega_2, \omega_3, \omega_4 \leq 1, \omega_1 + \omega_2 = 1, \omega_3 + \omega_4 = 1$ .

## 2.7 Multicast Tree Evaluation

The  $i_{th}$  user utility  $UU_i^T$ , the  $z_{th}$  network provider utility  $NU_z^T$ , all user utility  $UU^T$ , all network provider utility  $NU^T$  along  $T_{sD}$ , the cost  $CT^T$  of  $T_{sD}$  and the comprehensive evaluation  $CE^T$  on  $T_{sD}$  are calculated as follows:

$$UU_i^T = \sum_{e_l \in T_{sD}} uu_{il} \times NE_{izl} \quad (31)$$

$$NU_z^T = \sum_{e_l \in T_{sD}} nu_{z_l} \times NE_{izl} \quad (32)$$

$$UU^T = \sum_i UU_i^T \quad (33)$$

$$NU^T = \sum_z NU_z^T \quad (34)$$

$$CT^T = \sum_{e_l \in T_{SD}} ct_l \times abw_l \quad (35)$$

$$CE^T = \beta_1 \times \frac{\Omega_1}{UU^T} + \beta_2 \times \frac{\Omega_2}{NU^T} + \beta_3 \times \frac{CT^T}{\Omega_3} \quad (36)$$

$$NE_{izl} = \begin{cases} > 1 & \text{Nash equilibrium} \\ 1 & \text{otherwise} \end{cases} \quad (37)$$

$\beta_1, \beta_2$  and  $\beta_3$  are the preference weights on the user utility, the network provider utility and the tree cost respectively,  $0 \leq \beta_1, \beta_2, \beta_3 \leq 1$ ,  $\beta_1 + \beta_2 + \beta_3 = 1$ ;  $\Omega_1, \Omega_2$  and  $\Omega_3$  are tuning factors, making  $\Omega_1/UU^T, \Omega_2/NU^T$  and  $CT^T/\Omega_3$  into the same magnitude order. According to the formula (36), the smaller the value of  $CE^T$ , the much possible for  $UU^T$  and  $NU^T$  to achieve or approach the Pareto optimum [16] under the Nash equilibrium, the much possible the minimum  $CT^T$  achieved or approached.

## 2.8 Mathematical Model

It is described as follows:

$$\text{maximize} \{ UU_i^T \} \quad (38)$$

$$\text{maximize} \{ UU^T \} \quad (39)$$

$$\text{maximize} \{ NU_z^T \} \quad (40)$$

$$\text{maximize} \{ NU^T \} \quad (41)$$

$$\text{maximize} \{ UU^T + NU^T \} \quad (42)$$

$$\text{minimize} \{ CT^T \} \quad (43)$$

s.t.

$$BW_{P_i} \geq BW_i^L \quad (44)$$

$$DL_{P_i} \leq DL_i^H \quad (45)$$

$$JT_{P_i} \leq JT_i^H \quad (46)$$

$$LS_{P_i} \leq LS_i^H \quad (47)$$

$$BW_{P_i} = \min_{e_l \in P_i} \{ abw_l \} \quad (48)$$

$$DL_{P_i} = \sum_{e_l \in P_i} dl_l \quad (49)$$

$$JT_{P_i} = \sum_{e_l \in P_i} jt_l \quad (50)$$

$$LS_{P_i} = 1 - \prod_{e_l \in P_i} (1 - ls_l) \quad (51)$$

$P_i$  is the path from  $v_s$  to  $v_{d_i}$  in  $T_{SD}$ .

## 2.9 Algorithm Description

It is described as follows:

Step1:  $IN = |D|, i = 1$ .

Step2: If  $i < IN$ , go to Step3, otherwise go to Step20.

Step3: Set the maximum bee number  $BN$ , the sent bee number by far  $j = 0$ , the acceptable baseline bid  $bd_l^0$  of each  $e_l$ , the bee sending period  $itv$ , the long distance bee life cycle  $ltv$ , the short distance bee life cycle  $stv$ , the hop counter  $hp = 0$ , the set of the constructed feasible paths from  $v_s$  to  $v_{d_i}$ :  $PS_i = \varnothing$ ; get  $pr_l^j$  for each  $e_l$  according to the formula (27).  $itv, ltv$  and  $stv$  are counted by hop.

Step4: If  $j < BN$ , go to Step5, otherwise go to Step18.

Step5: If  $hp$  can be divided by  $itv$  exactly, send a long distance  $Be_j$  from  $v_s$ , otherwise a short distance  $Be_j$ .

Step6: Set the initial information carried by  $Be_j$  as follows: bandwidth  $bw = \infty$ , delay  $dl = 0$ , delay jitter  $jt = 0$ , error rate  $ls = 0$ , the current node  $cn = v_s$ , the current path  $P_c = \{v_s\}$ , the set of those edges connecting with  $cn$ :  $ne = \varnothing$ , the candidate edge set for the next hop:  $ce = \varnothing$ .

Step7: Put all edges connecting with  $cn$  into  $ne$ ; delete those edges from  $ne$  which cause loop, that is,  $ne = ne - \{e_l | e_l \in ne \wedge an(e_l) \in P_c\}$ ,  $an(e_l)$  represents another node of  $e_l$  except  $cn$ .

Step8: If  $Be_j$  is long distance and  $hp > ltv$  or  $Be_j$  is short distance and  $hp > stv$ ,  $Be_j$  died, go to Step17; otherwise, go to Step9.

Step9: If  $ne = \varnothing$ , go to Step14, otherwise select one  $e_l$  from  $ne$  at random.

Step10: If  $\min\{bw, abw_l\} < BW_i^L$  or  $dl + dl_l > DL_i^H$  or  $jt + jt_l > JT_i^H$  or  $1 - (1 - ls)(1 - ls_l) > LS_i^H$ ,  $ne = ne - \{e_l\}$ , go to Step9; otherwise, get the loaded level of  $e_l$  by the formula (1).

Step11: If  $e_l$  is high-loaded, the  $i_{th}$  user determines its bid  $bd_l$  to  $e_l$  from  $\{bd_{ie}, bd_{ig}, bd_{if}, bd_{ip}\}$  according to its  $Q_{il}$  got by the formula (13), go to Step12; otherwise, get  $p_l$  according to the formula (2) or (3) if  $e_l$  is low-loaded or moderate-loaded, go to Step13.

Step12: If  $bd_i < bd_i^0$ ,  $ne = ne - \{e_l\}$ , go to Step9; otherwise,  
 $p_l = bd_i, bd_i^0 = bd_i$ .

Step13: Get  $uu_{il}$  and  $nu_{-j}$  according to the formula (15) and (23), the user and the network provider play game on  $e_l$  according to section 2.5: if the Nash equilibrium is achieved and the gaming strategy is  $\langle \text{accept, provide} \rangle$ ,  $ce = ce \cup \{e_l\}$  and  $ne = ne - \{e_l\}$ ; otherwise,  $ne = ne - \{e_l\}$  and go to Step9.

Step14: If  $ce = \varnothing$ ,  $Be_j$  died, go to Step17; otherwise, select one  $e_l$  from  $ce$  as the next hop by  $pr_l^j : bw = \min\{bw, abw_l\}$ ,  $dl = dl + dl_l$ ,  $jt = jt + jt_l$ ,  $ls = 1 - (1 - ls)(1 - ls_l)$ ,  $cn = an(e_l)$ ,  $P_c = P_c \cup \{e_l\} \cup \{cn\}$ ,  $ne = \varnothing$ ,  $ce = \varnothing$ ,  $hp = hp + 1$ .

Step15: If  $cn \neq v_{d_i}$ , go to Step7.

Step16:  $PS_i = PS_i \cup \{P_c\}$ .

Step17:  $j = j + 1$ , update  $pr_l^j$  for each  $e_l \in P_c$  according to the formula (28), go to Step4.

Step18: If  $PS_i = \varnothing$ , routing failed and the algorithm ends.

Step19:  $i = i + 1$ , go to Step2.

Step20: Set the maximum number of the constructed feasible multicast tree  $TN$ , the current number of the constructed feasible multicast tree  $tn = 0$ , the current optimal multicast tree  $T_{sD_{bt}} = \varnothing$  and  $CE^{T_{sD_{bt}}} = \infty$ .

Step21: If  $tn = TN$ , go to Step25.

Step22: Take one path from each  $PS_i$  randomly and construct a feasible multicast tree  $T_{sD_m}$  with them. If there exists any cycle in  $T_{sD_m}$ , do cycle elimination.

Step23: Calculate  $CE^{T_{sD_m}}$  according to the formula (36): if  $CE^{T_{sD_m}} < CE^{T_{sD_{bt}}}$ ,  $T_{sD_{bt}} = T_{sD_m}$  and  $CE^{T_{sD_{bt}}} = CE^{T_{sD_m}}$ .

Step24:  $tn = tn + 1$ , go to Step21.

Step25: If  $CE^{T_{sD_{bt}}} < \infty$ , output  $T_{sD_{bt}}$  as the problem solution, routing succeeded; otherwise, routing failed. The algorithm ends.

### 3. Performance Evaluation and Conclusion

Simulated implementation of the proposed QoS multicast routing scheme in this paper has been done on NS2 (Network Simulator 2). Some performance indexes have been evaluated, such as QoS multicast routing request succeeded rate (RSR), user utility (UU), network provider utility (NU), comprehensive utility (CU=UU+NU) and ratio of the Pareto optimum under the Nash equilibrium (RPN). Table 1 is the comparison results between the proposed scheme (denoted as B) and the SPF (Shortest Path First) based one (denoted as S) when doing simulation over the

CERNET topology. It can be concluded that the proposed scheme has better performance than the SPF based one. In future, its prototype system will be developed to improve its practicality.

**Table 1. Performance Comparison**

Index	RSR	UU	NU	CU	RPN
B:S	1.36	1.65	1.54	1.62	2.12

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