



# Secrecy Sum Rate Optimization in MIMO NOMA OSTBC Systems with Imperfect Eavesdropper CSI

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**Abstract.** In this research, we investigate the secrecy sum rate optimization problem for a multiple-input multiple-output (MIMO) non-orthogonal multiple access (NOMA) system with orthogonal space-time block codes (OSTBC). We construct a model where the transmitter and the relay send information by employing OSTBC, while both the source and the relay have imperfect channel state information (CSI) of the eavesdropper. The precoders and the power allocation scheme are jointly designed to maximize the achievable secrecy sum rate subject to the power constraints and the minimum transmission rate requirements of the weak user. To solve this non-convex problem, we propose the constrained concave convex procedure (CCCP)-based iterative algorithm and the alternative optimization (AO) method, where the closed-form expression for power allocation is derived. The simulation results demonstrate the superiority of our proposed scheme.

**Keywords:** Multiple-input Multiple-output (MIMO) · Relay  
Non-orthogonal multiple access (NOMA) · Orthogonal space-time  
block codes (OSTBC) · Secrecy sum rate · Imperfect CSI

## 1 Introduction

With the popularization of smart terminals and the rapid development of 5G wireless communication technology, people are looking for a method to take full use of spectrum resources. Nowadays, non-orthogonal multiple access (NOMA) scheme can not only meet the requirements of wireless communication for spectrum utilization, but also achieve better throughput gain. In [1], the NOMA technique is applied in the multiple-input multiple-output (MIMO) systems.

With the aid of linear processing at the receiver, the orthogonal space-time block codes (OSTBC) technique for MIMO NOMA systems can achieve full diversity and full rate using [2]. Meanwhile, since the existence of potential

eavesdroppers in the current communication system, wireless information is susceptible to be eavesdropped. Thus, effective measures should be taken to deal with the threat of eavesdropping events in MIMO NOMA systems [4]. However, to the best of our knowledge, the secure precoding scheme in the MIMO NOMA robust systems with OSTBC has not been studied yet.

In this paper, a MIMO NOMA robust system is investigated to ensure secure information transmission between the transmitter and relay, which employ OSTBC. The precoder and power allocation scheme are jointly designed to maximize achievable secrecy sum rate. Since the optimization problem is non-convex, we propose the constrained concave convex procedure (CCCP)-based iterative algorithm and the AO method, where the closed-form expression for power allocation is derived. The remainder of the paper is organized as follows. In Sect. 2, we describe the system model and problem formulation. Section 3 presents the proposed algorithm to solve the precoder and power allocation problem. Simulation results are provided in Sects. 4 and 5 concludes this paper.

## 2 System Model and Problem Formulation

As shown in Fig. 1, we consider a MIMO NOMA system consisting of one transmitter, one relay, two legal users  $U_1, U_2$ , and a potential eavesdropper  $U_3$ , equipped with  $M_s, M_r, M_1, M_2, M_3$  antennas, respectively. The channel coefficient from the transmitter to relay is denoted as  $\mathbf{H}_r$ , and the ones from the relay to  $U_1, U_2$  and  $U_3$  are  $\mathbf{H}_1, \mathbf{H}_2$  and  $\mathbf{H}_3$ , respectively. In this system, the transmitter tends to send information to  $U_1$  and  $U_2$  safely.

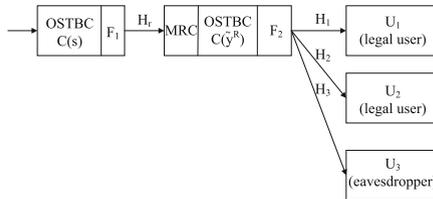


Fig. 1. Precoding of OSTBC for MIMO relay system.

We assume that the transmitter knows the perfect CSI of the relay,  $U_1$  and  $U_2$  while the CSI of  $U_3$  is imperfect. Thus, the channel response  $\mathbf{H}_3$  is defined as

$$\mathbf{H}_3 = \hat{\mathbf{H}}_3 + \Delta\mathbf{H}_3 \tag{1}$$

where  $\hat{\mathbf{H}}_3$  denotes the estimation of the channel from the transmitter to the eavesdropper,  $\Delta\mathbf{H}_3$  refers to the channel uncertainty of  $\mathbf{H}_3$ , which is bounded by the elliptical regions, i.e.,  $\mathcal{H}_3$

$$\mathcal{H}_3 = \{\Delta\mathbf{H}_3 | Tr(\Delta\mathbf{H}_3^\dagger \mathbf{Q}_3 \Delta\mathbf{H}_3) \leq 1\} \tag{2}$$

where  $\mathbf{Q}_3$  is assumed to be known and determine the qualities of CSI.

The S-R-D signal transmission procedure takes place in two steps. In the first phase, the received signal at the relay is expressed as  $\mathbf{Y}_r = \mathbf{H}_r \mathbf{F}_1 \mathbf{C}(\mathbf{s}) + \mathbf{N}_r$ , where  $\mathbf{F}_1 \in \mathbb{C}^{M_s \times M_s}$  denotes the transmitter's precoder;  $\mathbf{N}_r$  refers to the Gaussian noise with  $\mathbf{N}_r \sim \mathcal{CN}(0, \sigma_r^2 \mathbf{I})$ ;  $\mathbf{C}(\mathbf{s}) \in \mathbb{C}^{M_s \times T}$  ( $\mathbf{C}(\mathbf{s}) \mathbf{C}^H(\mathbf{s}) = \tilde{a} P_s \mathbf{I}_{M_s}$ ) is the OSTBC matrix with a code specific constant  $\tilde{a}$ .

We assume that the  $U_1$ 's information corresponds to the symbols  $x_{1,1}$  and  $x_{1,2}$ , the  $U_2$ 's information corresponds to the symbols  $x_{2,1}$  and  $x_{2,2}$ . The encoding and transmission sequence at the transmitter for the MIMO NOMA system with OSTBC is shown in Table 1 [3], where  $T = 2$ ,  $M_s = 2$ .

**Table 1.** Transmitter schematic of OSTBC

Antenna 1	Antenna 2
$t_1 : s_1 = \sqrt{\phi_1 P_s} x_{1,1} + \sqrt{\phi_2 P_s} x_{2,1},$	$s_2 = \sqrt{\phi_1 P_s} x_{1,2} + \sqrt{\phi_2 P_s} x_{2,2}$
$t_2 : -s_2^* = -\sqrt{\phi_1 P_s} x_{1,2}^* - \sqrt{\phi_2 P_s} x_{2,2}^*,$	$s_1^* = \sqrt{\phi_1 P_s} x_{1,1}^* + \sqrt{\phi_2 P_s} x_{2,1}^*$

As presented in Table 1,  $s_1$  and  $s_2$  are simultaneously transmitted to the relay in the time slot  $t_1$ . In the next time slot  $t_2$ ,  $s_1^*$  and  $-s_2^*$  are transmitted.  $\phi_1$  and  $\phi_2$  are the power allocation factors of  $U_1, U_2$ , which satisfy  $\phi_1 + \phi_2 = 1$ .  $P_s$  is the transmission power of the transmitter and  $E\{|x_{j,i}|^2\} = 1$ ,  $i, j \in \{1, 2\}$ .

Since the relay processes  $\mathbf{Y}_r$  with maximum ratio combiner (MRC), thus, the received signal at the relay can be written as [5]

$$y_k^R = \|\mathbf{H}_r \mathbf{F}_1\| z_k + n_{r,k}, i \in \{1, \dots, K\} \quad (3)$$

where  $z_k = \sqrt{\frac{\phi_1 P_s}{K}} x_{1,k} + \sqrt{\frac{\phi_2 P_s}{K}} x_{2,k}$ ,  $n_{r,k} \sim \mathcal{CN}(0, \sigma_r^2)$  refers to the AWGN at the relay for the  $k$ th S-R SISO channel and follows complex Gaussian distribution with zero-mean and variance  $\sigma_r^2$ . The relay normalizes  $\{y_k^R\}_{k=1}^K$  yielding

$$\tilde{y}_k^R = \frac{y_k^R}{\sqrt{E\{|y_k^R|^2\}}} = \frac{\|\mathbf{H}_r \mathbf{F}_1\| z_k + n_{r,k}}{\sqrt{\|\mathbf{H}_r \mathbf{F}_1\|^2 + \sigma_r^2}} \quad (4)$$

In the second phase, the destination receive signal  $\mathbf{Y}_d = \mathbf{H}_j \mathbf{F}_2 \mathbf{C}(\tilde{\mathbf{y}}^R) + \mathbf{N}_j^d$ , where  $\mathbf{C}(\tilde{\mathbf{y}}^R) \in \mathbb{C}^{M_r \times T}$  is the OSTBC formed from  $\tilde{\mathbf{y}}^R = [\tilde{y}_1^R, \dots, \tilde{y}_K^R]$ ;  $\mathbf{F}_2 \in \mathbb{C}^{M_r \times M_r}$  is the relay precoder;  $\mathbf{H}_j$ ,  $j \in \{1, 2, 3\}$  is the R-D MIMO channel and  $\mathbf{N}_j^d$  is the matrix of AWGN samples at the destination with zero mean and variance  $\tilde{\sigma}_j^2$ .

As in the case of  $k$ th S-R SISO channel, the signal received by the destination in the  $k$ th R-D SISO channel is given by

$$y_k^D = \|\mathbf{H}_j \mathbf{F}_2\| \tilde{y}_k^R + n_{2,k}, \forall k \quad (5)$$

where  $n_{j,k} \sim \mathcal{CN}(0, \sigma_j^2)$  is the AWGN at the relay for the  $k$ th S-R SISO channel. Using (4), (5) can be expressed as

$$y_k^D = \frac{\|\mathbf{H}_j \mathbf{F}_2\| \| \mathbf{H}_r \mathbf{F}_1 \| z_k + \|\mathbf{H}_j \mathbf{F}_2\| n_{r,k}}{\sqrt{\|\mathbf{H}_r \mathbf{F}_1\|^2 + \sigma_1^2}} + n_{j,k} \quad (6)$$

Therefore, the SNR at the destination is given as

$$y_k^D = \frac{\|\mathbf{H}_j \mathbf{F}_2\| \| \mathbf{H}_r \mathbf{F}_1 \| z_k + \|\mathbf{H}_j \mathbf{F}_2\| n_{r,k}}{\sqrt{\|\mathbf{H}_r \mathbf{F}_1\|^2 + \sigma_1^2}} + n_{j,k} \quad (7)$$

We assume that  $\|\mathbf{H}_1 \mathbf{F}_2\|^2 \geq \|\mathbf{H}_2 \mathbf{F}_2\|^2 \geq \|\mathbf{H}_3 \mathbf{F}_2\|^2$ , user  $U_1$  is the strong user and user  $U_2$  is the weak user. At the strong user  $U_1$ , the signal-to-noise ratio (SNR) to decode signals of the weak user  $U_2$  is

$$\gamma_1^2 = \frac{\frac{\phi_2 P_s}{K} \|\mathbf{H}_1 \mathbf{F}_2\|^2 \|\mathbf{H}_r \mathbf{F}_1\|^2}{\frac{\phi_1 P_s}{K} \|\mathbf{H}_r \mathbf{F}_1\|^2 \|\mathbf{H}_1 \mathbf{F}_2\|^2 + \|\mathbf{H}_r \mathbf{F}_1\|^2 \sigma_1^2 + \|\mathbf{H}_1 \mathbf{F}_2\|^2 \sigma_2^2 + \sigma_1^2 \sigma_2^2} \quad (8)$$

$$= \frac{\frac{\phi_2 P_s}{K} \gamma_1 \gamma}{\frac{\phi_1 P_s}{K} \gamma_1 \gamma + \gamma_1 + \gamma + 1}. \quad (9)$$

At the weak user  $U_2$ , the SNR to detect its own signals is

$$\gamma_2^2 = \frac{\frac{\phi_2 P_s}{K} \gamma_2 \gamma}{\frac{\phi_1 P_s}{K} \gamma_2 \gamma + \gamma_2 + \gamma + 1}. \quad (10)$$

The minimum SNR requirement of the weak user  $U_2$  is denoted as  $\gamma_0$ , due to  $\gamma_1^2 \geq \gamma_2^2$ , the strong user  $U_1$  can remove signals of  $U_2$ . After successive interference cancelation (SIC), the SNR of  $U_1$  to detect its own signals is given by

$$\gamma_1^1 = \frac{\frac{\phi_1 P_s}{K} \gamma_1 \gamma}{\gamma_1 + \gamma + 1} \quad (11)$$

Then at the eavesdropper  $U_3$ , the SNR to detect the signals of  $U_1$  and  $U_2$  is

$$\gamma_3^{1,2} = \frac{\frac{P_s}{K} \gamma_3 \gamma}{\gamma_3 + \gamma + 1}. \quad (12)$$

where  $\gamma = \frac{\|\mathbf{H}_r \mathbf{F}_1\|^2}{\sigma_r^2}$ ,  $\gamma_j = \frac{\|\mathbf{H}_j \mathbf{F}_2\|^2}{\sigma_j^2}$ ,  $j \in \{1, 2, 3\}$ . The transmit powers of the source and relay per OSTBC block can be given by  $P_s = \tilde{a} P_s \text{Tr}(\mathbf{F}_1 \mathbf{F}_1^H)$  and  $P_r = \tilde{a} P_s \text{Tr}(\mathbf{F}_2 \mathbf{F}_2^H)$ , where  $P_s = P_r$ .

Based on (11), (2) and (12), the achievable secrecy sum rate can be calculated as

$$R_s = \log_2(1 + \gamma_1^1) + \log_2(1 + \gamma_2^2) - \log_2(1 + \gamma_3^{1,2}) \quad (13)$$

### 3 Precoder and Power Optimization

The secrecy sum rate optimization problem can be formulated as

$$\begin{aligned} \max_{\{\mathbf{W}_1, \mathbf{W}_2, \gamma_1, \gamma_2, \phi_1, \phi_2\}} \quad & \log_2(1 + \gamma_1^1) + \log_2(1 + \gamma_2^2) \\ & - \log_2(1 + \gamma_3^{1,2}) \end{aligned} \quad (14a)$$

$$\text{s.t.} \quad \gamma_2^2 \geq \gamma_0, \quad (14b)$$

$$\phi_1 + \phi_2 = 1, \quad (14c)$$

$$0 \leq \phi_1 \leq 1, \quad (14d)$$

$$0 \leq \phi_2 \leq 1, \quad (14e)$$

$$\frac{\|\mathbf{H}_r \mathbf{F}_1\|^2}{\sigma_r^2} = \gamma, \quad (14f)$$

$$\frac{\|\mathbf{H}_1 \mathbf{F}_2\|^2}{\sigma_1^2} \geq \gamma_1, \quad (14g)$$

$$\frac{\|\mathbf{H}_2 \mathbf{F}_2\|^2}{\sigma_2^2} \geq \gamma_2, \quad (14h)$$

$$\text{Tr}(\mathbf{F}_1 \mathbf{F}_1^H) \leq \frac{1}{\bar{a}}, \text{Tr}(\mathbf{F}_2 \mathbf{F}_2^H) \leq \frac{1}{\bar{a}}, \quad (14i)$$

$$\text{Tr}(\mathbf{H}_1^H \mathbf{H}_1 \mathbf{W}_2) \geq \text{Tr}(\mathbf{H}_2^H \mathbf{H}_2 \mathbf{W}_2), \quad (14j)$$

$$\text{Tr}(\mathbf{H}_2^H \mathbf{H}_2 \mathbf{W}_2) \geq \text{Tr}(\mathbf{H}_3^H \mathbf{H}_3 \mathbf{W}_2) \quad (14k)$$

$$\frac{\|\mathbf{H}_3 \mathbf{F}_2\|^2}{\sigma_3^2} \leq \gamma_3 \quad (14l)$$

Next, we employ the S-procedure to convert the constraints (14i) into linear matrix inequalities (LMIs).

$$\begin{cases} \forall \Delta \mathbf{H}_3 : \text{Tr}(\Delta \mathbf{H}_3^\dagger \mathbf{Q}_3 \Delta \mathbf{H}_3) \leq \theta_3 \\ \text{Tr}(\mathbf{H}_3^\dagger \mathbf{W}_2 \mathbf{H}_3) - \gamma_3 \sigma_3^2 \leq 0 \end{cases} \quad (15)$$

Then we rewrite it as follows:

$$\begin{cases} \forall \Delta \mathbf{h}_3 : \Delta \mathbf{h}_3^\dagger (\mathbf{I} \otimes \mathbf{Q}_3) \Delta \mathbf{h}_3 - \theta_3 \leq 0 \\ \Delta \mathbf{h}_3^\dagger (\mathbf{I} \otimes \mathbf{Q}_3) \Delta \mathbf{h}_3 + 2 \text{Re}\{((\mathbf{I} \otimes \mathbf{Q}_3) \mathbf{h}_3^\dagger) \Delta \mathbf{h}_3\} + \mathbf{h}_3^\dagger (\mathbf{I} \otimes \mathbf{Q}_3) \mathbf{h}_3 - \gamma_3 \sigma_3^2 \leq 0 \end{cases} \quad (16)$$

$$\begin{bmatrix} \lambda_3 (\mathbf{I} \otimes \mathbf{Q}_3) - (\mathbf{I} \otimes \mathbf{W}_2) & -(\mathbf{I} \otimes \mathbf{W}_2) \mathbf{h}_3 \\ -\mathbf{h}_3^\dagger (\mathbf{I} \otimes \mathbf{W}_2) & \gamma_3 \sigma_3^2 - \lambda_3 \theta_3 - \mathbf{h}_3^\dagger (\mathbf{I} \otimes \mathbf{Q}_3) \mathbf{h}_3 \end{bmatrix} \succeq 0 \quad (17)$$

where  $\lambda_3 \geq 0$  is a slack variable,  $\mathbf{h}_3 = \text{vec}(\mathbf{H}_3)$ .

The problem is recast as

$$\begin{aligned}
 & \max_{\{\mathbf{W}_1, \mathbf{W}_2, \gamma_1, \gamma_2, \phi_1, \phi_2, \lambda_3\}} && \log_2(1 + \gamma_1^1) + \log_2(1 + \gamma_2^2) \\
 & && - \log_2(1 + \gamma_3^{1,2}) && (18a) \\
 \text{s.t.} & && \text{Tr}(\mathbf{D}\mathbf{W}_1) = \gamma, && (18b) \\
 & && \text{Tr}(\mathbf{A}\mathbf{W}_2) \geq \gamma_1 \sigma_1^2, && (18c) \\
 & && \text{Tr}(\mathbf{B}\mathbf{W}_2) \geq \gamma_2 \sigma_2^2, && (18d) \\
 & && \text{Tr}(\mathbf{W}_1) \leq \frac{1}{a}, \text{Tr}(\mathbf{W}_2) \leq \frac{1}{a}, && (18e) \\
 & && \text{Tr}(\mathbf{A}\mathbf{W}_2) \geq \text{Tr}(\mathbf{B}\mathbf{W}_2), && (18f) \\
 & && \text{Tr}(\mathbf{B}\mathbf{W}_2) \geq \text{Tr}(\mathbf{C}\mathbf{W}_2), && (18g) \\
 & && (14b) - (14e), (17). && (18h)
 \end{aligned}$$

where  $\gamma_0$  denotes the minimum SNR requirement of the weak user  $U_2$ ;  $\mathbf{W}_1 = \mathbf{F}_1^H \mathbf{F}_1$ ,  $\mathbf{W}_2 = \mathbf{F}_2^H \mathbf{F}_2$ ,  $\mathbf{A} = \mathbf{H}_1^H \mathbf{H}_1$ ,  $\mathbf{B} = \mathbf{H}_2^H \mathbf{H}_2$ ,  $\mathbf{C} = \mathbf{H}_3^H \mathbf{H}_3$ ,  $\mathbf{D} = \mathbf{H}_r^H \mathbf{H}_r$ . Because the objective and constraints are non-convex, problem (18) can not be directly solved by convex method. As far as we know, (18) has no global optimal solution, so we will use an effective method to attain the local optimal solution.

By introducing slack variables  $\{a, b, c\}$  such that  $\gamma_1^1 \geq a$ ,  $\gamma_2^2 \geq b$ ,  $\gamma_3^{1,2} \leq c$ , (18) is equivalently recast as

$$\begin{aligned}
 & \max_{\{\mathbf{W}_1, \mathbf{W}_2, \gamma_1, \gamma_2, \phi_1, \phi_2, a, b, c\}} && \log_2(1 + a) + \log_2(1 + b) \\
 & && - \log_2(1 + c) && (19a) \\
 \text{s.t.} & && \gamma_2^2 \geq \gamma_0, && (19b) \\
 & && \gamma_1^1 \geq a, && (19c) \\
 & && \gamma_2^2 \geq b, && (19d) \\
 & && \gamma_3^{1,2} \leq c, && (19e) \\
 & && (18b) - (18h). && (19f)
 \end{aligned}$$

Based on (12), (19e) is expressed as

$$\frac{1}{\gamma_3} + \frac{1}{\gamma} + \frac{1}{\gamma_3 \gamma} \geq \frac{P_s}{cK} \tag{20a}$$

$$\tau_3 + \tau_{min} + t_3 \geq \frac{P_s}{cK} \tag{20b}$$

$$\tau_3 \gamma_3 \leq 1 \tag{20c}$$

$$\tau_{min} \gamma \leq 1 \tag{20d}$$

$$t_3 \gamma_3 \gamma \leq 1 \tag{20e}$$

Equation (20e) is expressed as

$$\begin{bmatrix} \mu_3 & t_3 \\ \gamma & \mu_3 \end{bmatrix} \succeq 0 \quad (21a)$$

$$\begin{bmatrix} \mu_{3,3} & 1 \\ 1 & \mu_{3,3} \end{bmatrix} \succeq 0 \quad (21b)$$

$$\mu_3 \mu_{3,3} \leq 1 \quad (21c)$$

Similarly, (19b), (19c), (19d) are expressed as

$$\frac{1}{\gamma_1} + \frac{1}{\gamma} + \frac{1}{\gamma_1 \gamma} \leq \frac{\phi_1 P_s}{aK} \quad (22a)$$

$$\tau_1 + \tau_{max} + t_1 \leq \frac{\phi_1 P_s}{aK} \quad (22b)$$

$$\frac{1}{\gamma_2} + \frac{1}{\gamma} + \frac{1}{\gamma_2 \gamma} \leq \frac{1}{b - \frac{\phi_1}{\phi_2}} \frac{\phi_2 P_s}{K} \quad (22c)$$

$$\tau_2 + \tau_{max} + t_2 \leq \frac{1}{b - \frac{\phi_1}{\phi_2}} \frac{\phi_2 P_s}{K} \quad (22d)$$

$$\frac{1}{\gamma_2} + \frac{1}{\gamma} + \frac{1}{\gamma_2 \gamma} \leq \left( \frac{1}{\gamma_0} - \frac{\phi_1}{\phi_2} \right) \frac{\phi_2 P_s}{K} \quad (22e)$$

$$\tau_2 + \tau_{max} + t_2 \leq \left( \frac{1}{\gamma_0} - \frac{\phi_1}{\phi_2} \right) \frac{\phi_2 P_s}{K} \quad (22f)$$

$$\tau_i \gamma_i \geq 1 \quad (22g)$$

$$\tau_{max} \gamma \geq 1 \quad (22h)$$

$$t_i \gamma_i \geq 1 \quad (22i)$$

Hyperbolic constraints (22g) and (22h) can be converted into convex forms

$$\tau_i + \gamma_i \geq \|[\sqrt{2}, \tau_i, \gamma_i]^T\| \quad (23a)$$

$$\tau_{max} + \gamma \geq \|[\sqrt{2}, \tau_{max}, \gamma]^T\| \quad (23b)$$

Equation (22i) can be expressed as

$$\begin{bmatrix} t_i & \mu_i \\ \mu_i & \gamma \end{bmatrix} \succeq 0 \quad (24a)$$

$$\begin{bmatrix} 1 & \mu_{i,i} \\ \mu_{i,i} & \gamma_i \end{bmatrix} \succeq 0 \quad (24b)$$

$$\mu_i + \mu_{i,i} \geq \|[\sqrt{2}, \mu_i, \mu_{i,i}]^T\| \quad (24c)$$

where  $i \in \{1, 2\}$ .

Because of the non-convexity of these functions:  $-\log_2(1+c)$ , (20c), (20d) and (21c), we can employ the first-order Taylor method to recast them, which are expressed as  $f(c, \bar{c})$ ,  $f(\tau_3, \bar{\tau}_3)$ ,  $f(\tau_{min}, \bar{\tau}_{min})$ ,  $f(\mu_{3,3}, \bar{\mu}_{3,3})$ , respectively.

Then problem (18) can be rewritten as

$$\begin{aligned}
 \max_{\{\mathbf{W}_1, \mathbf{W}_2, \gamma_1, \gamma_2, \phi_1, \phi_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t}\}} & \log_2(1+a) + \log_2(1+b) \\
 & - f(c, \bar{c}) \tag{25a} \\
 \text{s.t.} & (22b), (22d), (22f), (23), \tag{25b} \\
 & (24), (20b), \tag{25c} \\
 & (21a), (21b), \tag{25d} \\
 & (18b) - (18h) \tag{25e} \\
 & f(\tau_3, \bar{\tau}_3), f(\tau_{min}, \bar{\tau}_{min}), f(\mu_{3,3}, \bar{\mu}_{3,3}). \tag{25f}
 \end{aligned}$$

To solve problem (25), we employ AO method which alternatively optimizes  $\phi_1$  and  $(\mathbf{W}_1, \mathbf{W}_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t})$ . Given  $\phi_1$ , problem (25) is convex with respect to  $(\mathbf{W}_1, \mathbf{W}_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t})$ , which can be solved by interior point method [6].

With given  $(\mathbf{W}_1, \mathbf{W}_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t})$ , we can obtain  $\phi_1$  as follow. Based on  $\gamma_2^2 \geq \gamma_0$ , the objective function is an increasing function with respect to  $\phi_1$ , then the closed-form solution of  $\phi_1$  can be achieved as

$$\phi_1 = \frac{1}{1+M} - M \frac{1 + Tr(\mathbf{W}_1 \mathbf{D}) + Tr(\mathbf{W}_2 \mathbf{A})}{0.5P_s(1+M)Tr(\mathbf{W}_2 \mathbf{B}) + Tr(\mathbf{W}_1 \mathbf{D})}. \tag{26}$$

The proposed AO method is shown in Algorithm 1 as below.

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**Algorithm 1** The Proposed AO Method to Solve Problem (21)

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- 1: **Initialization:**  $n = 0$  and  $\phi_1^{(0)}$  and an accuracy parameter  $\epsilon$ ;
  - 2: **Repeat:**
    - Solve problem (21) to update  $(\mathbf{W}_1, \mathbf{W}_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t})^{(n)}$ , with  $\phi_1^{(n)}$  fixed;
    - Use (26) to update  $\phi_1^{(n+1)}$  with  $(\mathbf{W}_1, \mathbf{W}_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t})^{(n)}$ ;
    - Update  $n = n + 1$ ;
  - 3: **Until:**  $|R^{(n)} - R^{(n-1)}| \leq \epsilon$ , where  $R^{(n)}$  is the objective value in the  $n$ th iteration.
- 

By solving problem (25), we get the optimal solution  $(\mathbf{W}_1, \mathbf{W}_2, a, b, c, \boldsymbol{\mu}, \boldsymbol{\tau}, \mathbf{t})^{(o)}$ . If the rank of  $\widehat{\mathbf{W}}^o$  equals to one, the optimal  $\mathbf{F}^o$  can be easily found. Otherwise, we can generate a suboptimal solution through the Gaussian random method in [9].

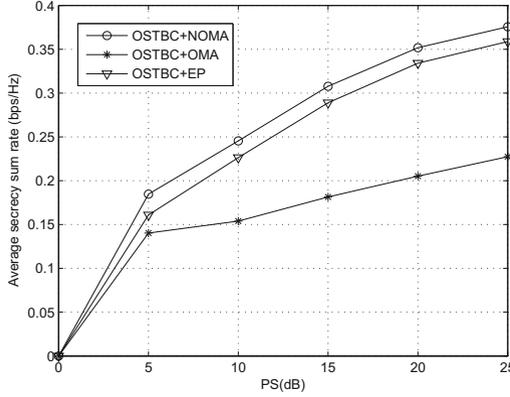
## 4 Simulation Results

Here, the simulation results are provided to validate the proposed robust precoding schemes with NOMA OSTBC are more effective than other cases.

In Fig. 2, we present the average achievable secrecy sum rates achieved by the proposed scheme, equal power allocation scheme and the conventional orthogonal multiple access scheme both with OSTBC (denoted as ‘‘OSTBC+NOMA’’,

“OSTBC+EP” “OSTBC+OMA”, respectively), versus the transmit power  $P_s$  with setting  $M_s = M_r = M_1 = M_2 = M_3 = 2$ ,  $\tilde{a} = 1$  and the minimum SNR requirement of the weak user  $\gamma_0 = 0.10$  dB.

It can be observed that our proposed “NOMA+OSTBC” scheme achieves better performance than the other two schemes for different  $P_s$ . This is because the superposition of signals to different users and SIC cause the bandwidth is explored more efficiently.

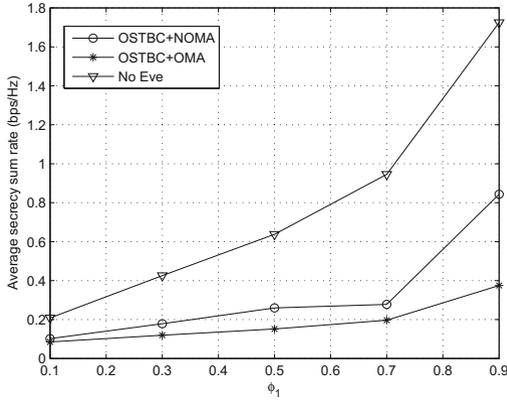


**Fig. 2.** The achievable secrecy sum rate versus  $P_s$ , obtained by “OSTBC+NOMA” scheme, the conventional “OSTBC+OMA” and “OSTBC+EP” scheme.

In Fig. 3, we show the effect of the power allocation factors of  $U_1$ , i.e.,  $\phi_1$ , where no eavesdropper situation (denoted as “No Eve”) is also compared. From Fig. 3, we find that “NOMA+OSTBC” scheme outperforms the “OSTBC+OMA” scheme with different  $\phi_1$ , for NOMA can achieve higher spectral efficiency and better user fairness than conventional OMA. Besides, larger  $\phi_1$  leads to higher secrecy sum rate. As  $\phi_1$  continues to increase, the performance gap between the “OSTBC+NOMA” and “OSTBC+OMA” becomes larger.

### 5 Conclusion

In this paper, the precoders and power allocation design for MIMO NOMA robust system with OSTBC is studied, where source and relay have imperfect CSI of the eavesdropper. To tackle the non-convexity of the optimization problem, we employ the CCCP-based algorithm and AO method to optimize the precoders and power allocation. The simulation results demonstrate the superiority of our proposed scheme.



**Fig. 3.** The achievable secrecy sum rate versus  $\phi_1$ , obtained by “OSTBC+NOMA” scheme, the conventional “OSTBC+OMA” scheme and “No Eve” scheme.

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