Secrecy Performance of Mobile Image Transmission Networks

Lingwei Xu¹, Xu Yu¹, Han Wang², Xinjie Wang³ and Jingjing Wang¹

¹Department of Information Science and Technology, Qingdao University of Science and Technology, Qingdao 266061, China; ²College of Physical Science and Engineering, Yichun University, Yichun 336000, China; ³College of Information and Control Engineering, Qingdao University of Technology, Qingdao 266520, China

Abstract. Due to the user mobility, the physical layer security of mobile image transmission networks is an important challenging task. In this paper, based on the classic Wyner wiretap model, the secrecy performance of mobile image transmission networks is investigated. We derive exact closed-form expressions for the average secrecy capacity (ASC). By Monte-Carlo simulations, we verify the accuracy of the derived theoretical results.

Keywords: mobile image transmission networks; physical layer security; average secrecy capacity.

1. Introduction

In recent years, based on user quality of experience (QoE), the mobile image transmission has attracted wide research interest [1,2]. In [3], the authors used Genetic Algorithm (GA) and Particle Swarm Optimization (PSO) techniques to improve the performance of the image steganography system.

Due to the user mobility, the physical layer security of wireless communications is an important challenging task. [4] designed a CP based secure wireless video data transmission. In [5], the security and privacy issues of multimedia services were investigated. Based on artificial-noise-aided beamforming, an optimized secure multi-antenna transmission approach was presented in [6]. [7] designed a multiple-input single-output downlink system to keep the message secret to the energy-harvesting receivers while maximizing the information rate at the information receiver.

However, in [4-7], the physical layer security performance is only considered for Rayleigh and Nakagami-m fading channels. Rayleigh and Nakagami-m fading channels are not fit to model the mobile image transmission [8]. To the best of our knowledge, the physical layer security of mobile image transmission networks has not been considered in the literature. In this paper, we use the average secrecy capacity (ASC) performance to measure the quality of mobile image transmission networks over 2-Nakagami fading channels. When we obtain the poor ASC performance, it means that the mobile image transmission is interrupted. We derive closed-form expressions for the ASC. By Monte-Carlo simulations, we verify the accuracy of the derived theoretical results.

The rest of the paper is organized as follows. The mobile Wyner wiretap model is presented in Section 2. The closed-form ASC expressions are derived in Section 3. Monte-
Carlo simulation results are provided in Section 4. Finally, some concluding remarks are given in Section 5.

2. The System Model

Figure 1. shows the mobile Wyner wiretap model. There is a mobile source (S), a mobile eavesdropper (E), and a mobile destination (D). They are all equipped with a single antenna.

![System Model Diagram](image-url)

We use \( h = h_k \), \( k \in \{ D, E \} \), to represent the complex channel coefficients. To represent the locations of the D and E relative to the S, the relative geometrical gain of the S→D channel is \( G_D \), and the relative geometrical gain of the S→E channel is \( G_E \) [9].

S transmits the image signal \( x \), D and E receive the signals as

\[
\begin{align*}
    r_D &= \sqrt{G_D} E h_d x + n_D \\
    r_E &= \sqrt{G_E} E h_e x + n_E
\end{align*}
\]

where \( E \) is the energy used by S, the mean and variance of \( n_D \) and \( n_E \) are 0 and \( N_0/2 \).

D receives the signal-to-noise ratio (SNR) as

\[
\gamma_D = K G_D \left| h_D \right|^2 \gamma
\]

\[
\gamma = \frac{E}{N_0}
\]

\[
\gamma_D = K G_D \gamma
\]

where \( K \) is the relative SNR gain.

E receives the SNR as

\[
\gamma_E = G_E \left| h_E \right|^2 \gamma
\]

\[
\gamma_E = G_E \gamma
\]

The cumulative distribution function of \( \gamma_E \) is then
where $\Gamma(\cdot)$ is the Gamma function, $m$ is the fading coefficient, and $\Omega$ is a scaling factor.

The corresponding probability density function is given as

$$f_{\gamma_1}(r) = \frac{1}{r^2 \prod_{i=1}^{2} \Gamma(m_i)} G_{2,0}^{2,0} \left[ \frac{r}{\gamma_k} \prod_{i=1}^{2} \frac{m_i}{\Omega_i} \omega_{1,\ldots,m_y} \right]$$

3. Average Secrecy Capacity

[10] gives the instantaneous secrecy capacity as

$$C_S = \max \{ \ln(1+\gamma_D) - \ln(1+\gamma_E), 0 \}$$

So the ASC is given as

$$C_S = \int_{0}^{\infty} \int_{0}^{\infty} C_S(\gamma_D, \gamma_E) f(\gamma_D, \gamma_E) d\gamma_D d\gamma_E$$

$$= \int_{0}^{\infty} \int_{0}^{\infty} C_S(\gamma_D, \gamma_E) f(\gamma_D, \gamma_E) d\gamma_D d\gamma_E$$

$$= \int_{0}^{\infty} \ln(1+\gamma_D) f(\gamma_D) F_E(\gamma_E) d\gamma_D$$

$$+ \int_{0}^{\infty} \ln(1+\gamma_E) f(\gamma_E) F_D(\gamma_D) d\gamma_E$$

$$- \int_{0}^{\infty} \ln(1+\gamma_E) f(\gamma_E) d\gamma_E$$

$$= M_1 + M_2 - M_3$$

With the help of [11], $M_i$ is given as
\[ M_1 = \prod_{j=1}^{N} \frac{1}{\Gamma(m_j) \prod_{j=1}^{N} \Gamma(m_j)} \times \]
\[ \int_0^\infty \left( 1 + \frac{1}{\gamma_D} \right) \frac{1}{\gamma_D} \frac{G_{D,0,2}^2 \left[ \frac{\gamma_D}{\gamma_D} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] G_{i,3}^2 \left[ \frac{\gamma_E}{\gamma_E} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] \right) d\gamma_D \]
\[ = \prod_{i=1}^{2} \frac{1}{\Gamma(m_i) \prod_{j=1}^{2} \Gamma(m_j)} \times \]
\[ \int_0^\infty \frac{G_{i,2,0}^{2,1} \left[ \frac{\gamma_D}{\gamma_D} \right] \frac{1}{\gamma_D} \frac{G_{D,0,2}^2 \left[ \frac{\gamma_D}{\gamma_D} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] G_{i,3}^2 \left[ \frac{\gamma_E}{\gamma_E} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] \right) \gamma_D^2}{d\gamma_D} \]
\[ = \prod_{i=1}^{2} \frac{1}{\Gamma(m_i) \prod_{j=1}^{2} \Gamma(m_j)} \times \]
\[ \prod_{i=1}^{2} \prod_{j=1}^{2} \frac{G_{i,2,0}^{1,3} \left[ \frac{\gamma_D}{\gamma_D} \right] \frac{1}{\gamma_D} \frac{G_{D,0,2}^2 \left[ \frac{\gamma_D}{\gamma_D} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] G_{i,3}^2 \left[ \frac{\gamma_E}{\gamma_E} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] \right) \gamma_D^2}{d\gamma_D} \]
\[ \text{(12)} \]

\[ M_2 \text{ is given as} \]
\[ M_2 = \prod_{i=1}^{2} \frac{1}{\Gamma(m_i) \prod_{j=1}^{2} \Gamma(m_j)} \times \]
\[ \prod_{i=1}^{2} \prod_{j=1}^{2} \frac{G_{i,2,0}^{1,3} \left[ \frac{\gamma_D}{\gamma_D} \right] \frac{1}{\gamma_D} \frac{G_{D,0,2}^2 \left[ \frac{\gamma_D}{\gamma_D} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] G_{i,3}^2 \left[ \frac{\gamma_E}{\gamma_E} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] \right) \gamma_D^2}{d\gamma_D} \]
\[ \text{(13)} \]

\[ M_3 \text{ is given as} \]
\[ M_3 = \prod_{j=1}^{2} \frac{1}{\Gamma(m_j)} \times \]
\[ \prod_{j=1}^{2} \prod_{j=1}^{2} \frac{G_{j,0}^{1,4} \left[ \frac{\gamma_E}{\gamma_E} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] \frac{1}{\gamma_D} \frac{G_{D,0,2}^2 \left[ \frac{\gamma_D}{\gamma_D} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] G_{j,3}^2 \left[ \frac{\gamma_E}{\gamma_E} \prod_{j=1}^{2} \frac{m_j}{\Omega_j} \right] \right) \gamma_D^2}{d\gamma_D} \]
\[ \text{(14)} \]

4. Numerical Results

In this section, we present Monte-Carlo simulations to confirm the derived analytical results.
Figure 2 shows the ASC performance. $\gamma = 10$ dB. Table 1. shows the simulation parameters. From Figure 2., it is found that the analytical results perfectly match with the simulation results. For a fixed $K$, the ASC performance is improved with increasing $m_D$ and decreasing $m_E$. The ASC performance for (2,1) is better than that of (1,1) and (1,2). Further, increasing $K$ improves the ASC performance. This is because a higher $K$ means that the $S \to D$ channel is better than the $S \to E$ channel.

Table 1. Simulation Parameters

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<th>$m_D$</th>
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<th>2</th>
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<td>1</td>
<td>1</td>
<td></td>
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<tr>
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<td>$G_E$</td>
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Fig. 2. ASC performance versus $K$.

Fig. 3. ASC performance versus $K$. 
Figure 3. presents the ASC performance versus $K$ with $(1,1)$. $\gamma=5$ dB, 10 dB, 15 dB, 20 dB, $G_D=G_r=5$ dB, $N_D=N_r=2$. It is found that the simulation results perfectly match the analytical results. For fixed $K$, increasing $\gamma$ improves the ASC performance. This is because the S→D channel is better than the S→E channel.

5. Conclusions

In this paper, the ASC performance of the mobile image transmission networks is investigated. We derive exact closed-form ASC expressions. They are verified via Monte-Carlo simulations. Increasing $K$ improves the quality of mobile image transmission networks.

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